# Sharing Models to Interpret Data

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#### Abstract

To understand new data, we share models or interpretations with others. This paper studies such exchanges of models in a community. The key assumption is that people adopt the interpretation in their community that best explains the data, given their prior beliefs. An implication is that interpretations evolve within communities to better fit prior knowledge, potentially making final reactions less accurate than initial reactions. When people entertain a rich set of possible interpretations, social learning often mutes reactions to data: the exchange of models leaves beliefs closer to priors than they were before, untethering beliefs from data. Our results shed light on why disagreements persist as new information arrives, popular theories link seemingly unrelated events, ideological bubbles need not be hermetically sealed, and firms and politicians can benefit from preemptively framing news.

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# **1** Introduction

We make sense of the world together. Why is the unemployment rate lower than expected? Why did one employee receive a promotion and not another? Why is the stock market skyrocketing? In response to such questions, we share not only information but also interpretations. Unemployment is lower than expected because "economic growth is strong" or because "there was a one-time blip in manufacturing". The employee received a promotion because "she is uniquely qualified" or "the firm is signaling that it values a particular set of skills". The stock market is rising because of "fundamentals" or "dumb money". What is the outcome of this exchange of interpretations? Does it push us towards the truth? How does with whom we talk affect the interpretation we settle on? And how might an interested party like a firm manager influence communication to shape ultimate interpretations?

This paper presents a formal framework for thinking about such exchanges of interpretations in a community. The basic ingredients of the model follow Schwartzstein and Sunderam (2021). Everyone shares a common prior  $\mu_0$  over states of the world  $\omega$  and observes a common, public history h. Aspects of the history are open to interpretation, meaning that people are willing to entertain different interpretations of the same data. Interpretations are represented by models, which we formalize as likelihood functions that link the history to states. In other words, interpretations capture different ways people can use the history to update their beliefs. When people are exposed to multiple interpretations, they adopt the one that best fits the data, fixing prior beliefs. People have a default interpretation d, represented by likelihood function  $\pi_d(h|\omega)$ , and come up with a single alternative interpretation—their initial reaction to the data—that they adopt if it is more compelling than their default interpretation, i.e., it better fits the data plus their prior.

In contrast to standard models where social learning is driven by the desire to learn others' private information, in our framework everyone shares the same information but learns from others' interpretations. People are exposed to the interpretations of others in their community and settle on the one that is most compelling. Formally, person *i* adopts the model she is exposed to *m* (represented by likelihood function  $\pi_m(h|\omega)$ ) if

$$m \in \arg \max_{\tilde{m} \in \left\{ d, m_i' \right\} \cup M_i} \underbrace{\Pr(h|\tilde{m}, \mu_0)}_{= \int \pi_{\tilde{m}}(h|\omega) d\mu_0(\omega)},$$

where  $m'_i$  represents the model person *i* comes up with initially and  $M_i$  is the set of models the person is exposed to in her community.<sup>1</sup> Thus, the key role of the community in our framework is to determine the set of models she is exposed to. Given this set of models, she picks the one that maximizes the probability of the history given her prior,  $Pr(h|m, \mu_0)$ . In Bayesian terms, the person acts as if she has a flat prior over the models she is exposed to and then selects the model that best fits the data and her prior, which is equivalent to selecting the model with the highest associated posterior probability. More intuitively, this assumption loosely captures ideas from the social sciences about what people find persuasive, including that people favor models that (i) have high "fidelity" to the data as emphasized in work on narratives (Fisher 1985); (ii) help with "sensemaking" as discussed in work on organizational behavior and psychology (Chater and Loewenstein (2016)); (iii) make the past feel more predictable (Schulz and Sommerville (2006); Gershman (2019)); and (iv) have the most "explanatory power" (Lombrozo (2016)).<sup>2</sup>

To see some key implications of this formulation, consider an example where a community of investors assesses a technology firm. The firm's fundamentals are either good or bad,  $\omega \in \{g, b\}$ , and investors in this community are optimistic, attaching prior probability  $\mu_0(g) = 0.75$  to fundamentals being good. Data comes out: h = "the firm's earnings this quarter were lower than expected and the aggregate economy entered a recession".

Investors consequently disagree about the firm's fundamentals because they use different models to interpret the data. Suppose that under the true model,  $m^T$ , lower than expected earnings are a negative signal about fundamentals— $\pi_{m^T}(\text{low earnings}|b) = 0.75 > 0.25 = \pi_{m^T}(\text{low earnings}|g)$ —but the aggregate economy is irrelevant for updating about the firm's fundamentals. Bayes' rule implies that the true posterior probability that the firm's fundamentals are good is  $\Pr(g|h, m^T) = 0.5$ . However, investors are willing to entertain alternative interpretations. Some initially come up with the true interpretation that the aggregate economy is irrelevant, but low earnings reduce the probability that the firm's fundamentals are good. Others think that low earnings are a particularly negative signal in a recession, following famed investor Warren Buffett's adage that "only when the tide goes out do you discover who's been swimming naked." For example, these investors could hold a model specifying that  $\pi_{m^B}(\text{low earnings}, \text{recession}|b) = .05$  and

<sup>&</sup>lt;sup>1</sup>We will use the terms community and network interchangeably.

<sup>&</sup>lt;sup>2</sup>Recent work (e.g., Barron and Fries (2022), Kwon et al. (2022)) experimentally tests and finds support for the assumption that people find better-fitting models more persuasive.

 $\pi_{m^B}(\text{low earnings, recession}|g) = .25 \times .05$ , which would imply that  $\Pr(g|h, m^B) \approx 0.43$ . Yet others believe that these kinds of technology firms always have low earnings in a recession, regardless of fundamentals:  $\pi_{m^A}(\text{low earnings, recession}|b) = \pi_{m^A}(\text{low earnings, recession}|g) = .05$ , which implies that  $\Pr(g|h, m^A) = 0.75$ . Suppose that the only restriction on the models investors are willing to entertain is that they agree with the true model on the marginal probabilities of a recession and of low earnings. Assuming that the population is sufficiently large that roughly every such interpretation is someone's initial reaction and that the community is sufficiently connected that the most compelling interpretation spreads throughout the population, we ask: which take goes viral?

Not the right one. When low earnings are more likely than recessions, the "always low in a recession" interpretation will eventually be held by all investors in this community because it is the best-fitting model consistent with the marginal probability of a recession. Social learning spreads an interpretation of the data under which investors' posterior on the firm's fundamentals equals their prior probability of 0.75, instead of the true posterior of 0.5.<sup>3</sup> As shown in Schwartzstein and Sunderam (2021), models that fit well imply the data is unsurprising, which means beliefs should not move much away from priors in response to it. In this example, investors' prior is that the firm likely has good fundamentals. The model that best fits their knowledge (i.e., their prior and the data) leads them to stick with their prior.

The example illustrates four main points. First, explanations linking events that are in truth unrelated can be more persuasive than the true model. For instance, the "always low in a recession" model, which links recessions and low earnings, fits the data better than the true model that they are independent events. In our framework, such "conspiratorial" models will tend to spread more easily than the truth. Indeed, the model investors end up holding is "maximally conspiratorial": it connects low earnings and the recession as strongly as possible in a way we make precise below.

Second, social learning *hardens* reactions to data: following the exchange of models, people are more certain they have the right explanation for the data in the sense of having a model with a higher value of  $Pr(h|m, \mu_0)$ . Exposure to others' models provides ways to explain the data that they may not find on their own. Thus, some investors could have been

<sup>&</sup>lt;sup>3</sup>As we show in Proposition 1 below, an additional assumption is required to guarantee that all investors hold this posterior given the restricted model space in this example. Proposition 2 shows that all investors will hold this posterior in a modified version of the example with an unrestricted model space.

persuaded of the true model prior to social learning, but they cannot be persuaded after because social learning provides them with a better explanation for the data.

Third, interpretations *evolve* in ways that often make final interpretations *less* accurate than initial reactions. Before social learning, some investors correctly interpret low earnings and put a low posterior probability on the state in which the firm's fundamentals are good. However, the exchange of models leads them to interpretations resulting in the belief that the fundamentals are likely to be good. In other words, the marketplace of models pushes people away from the right interpretation. This evolution of beliefs highlights a key distinction between our formulation and models where people simply believe what they want to believe. In these alternative formulations, if investors prefer accounts that the firm's fundamentals are good, then their *initial* reactions will exhibit that preference.

A fourth point is that social learning has a tendency to *mute* reactions—bringing posterior beliefs closer to prior beliefs—by increasing the chances people are exposed to models that explain why the data is unsurprising and hence beliefs should not move. Put differently, the exchange of models untethers beliefs from data that is open to interpretation.

Untethering appears to be an important feature of many real-world settings. For instance, despite a large amount of available information and strong incentives for agricultural firms to persuade them otherwise, nearly half of people around the world believe genetically modified foods (GMOs) are unsafe.<sup>4</sup> Consistent with our model, the persistence of these beliefs does not mean that people do not react to new information. They do react, but the impact of information tends to fade quickly, with people returning to their previous views. In our framework, the disconnect between data that is open to interpretation and long-run beliefs is driven by the adoption of models through social learning.

Section 3 studies communities formed on the basis of shared beliefs, where people with similar initial reactions to the data exchange models. Such communities are common—for instance, groups often form based on beliefs that one political party governs better than others—and have likely become easier to form over time due to technology like social media. To illustrate the intuitions that emerge, consider the example above, and suppose investors who initially interpret the data as suggesting firm fundamentals are good all talk to each other, while those whose initial interpretations suggest fundamentals are bad all talk to each other. We show that social learning then generates disagreement: while they all

<sup>&</sup>lt;sup>4</sup>See, e.g., Pew surveys here (link).

held the same prior beliefs, members of the "good fundamentals" and "bad fundamentals" communities end up disagreeing despite being exposed to the same information. Investors in the "good fundamentals" community converge on models that bring their beliefs closer to the 75% conditional prior probability they attached to the firm being good, while those in the "bad fundamentals" community converge to a probability less than 50%. As they exchange models, members of each community become less persuadable to arguments made outside their community (beliefs are hardened) and hold beliefs that are less tethered to the data (beliefs are muted).

We next document stylized evidence consistent with these predictions from a socialmedia network for stock market investors. Previous work has documented that investors tend to form communities with other investors who are similarly optimistic or pessimistic about a given stock (Cookson et al. (2022)). We show that optimistic investors become less optimistic immediately after a negative earnings surprise, but they quickly revert back to being optimistic. Pessimistic investors behave analogously. In our framework, these dynamics are driven by the spread of interpretations within the optimistic and pessimistic communities. Within each community, investors are exposed to interpretations of the data that make it less surprising, allowing disagreement to persist in the face of new information.

In Section 4, we show that inaccurate beliefs and disagreement can persist even as people communicate across communities and issues. We first consider communication across communities, drawing a distinction between weak and strong exposure to beliefs. We say a person is weakly exposed to a belief if she is aware of a single model that when combined with the data implies that belief. She is strongly exposed to a belief if she is aware of all models implying that belief. We think of communication within communities as strong exposure and communication across communities as weak exposure. Under this view, members of a community can be aware that people outside their community have different beliefs, but they will be unpersuaded by the interpretations of the data they know in favor of those different beliefs. In other words, ideological bubbles or echo chambers need not be hermetically sealed. People in a community can be exposed to a few interpretations from outside the community without finding those interpretations compelling.

We then study communication across issues, showing that it can lead to polarization. If communities are formed based on one issue, the exchange of interpretations leads to a divergence across communities of beliefs on a second issue. Thus, members of two communities can end up disagreeing on issues that were not central to their formation, despite the fact they are interpreting the same data. Such disagreement is consistent with the "polarization of reality" documented by Alesina et al. (2020).

Section 5 studies the implications of these results for how someone should manage communication. We show that providing people with a favored interpretation before social learning—i.e., "getting in front of the news"—is valuable in our framework. It helps the communications manager inoculate people against finding compelling models that support alternative beliefs. We next consider situations where the manager directly influences what communication takes place, for instance by restricting meeting attendance. We show that the communications manager faces a tradeoff between getting people to agree on a model and promoting a specific action. To create agreement on a model, the manager wants everyone to share interpretations, which leads to the widespread adoption of a model suggesting that there is little to learn from the data. In contrast, if the manager wants people to take a particular action, she wants only models that support that action to be shared.

Finally, we sketch some applications of our results in Section 6. We first study implications for how firm managers should run meetings. The traditional view in economics is that meetings enable information exchange (e.g., Dessein and Santos (2006)). In contrast, in our framework meetings serve to help workers interpret shared information, a view that builds on a large literature in organizational studies arguing that sensemaking is a central activity of organizations (e.g., Weick (1995)). We then consider why disagreement persists in the face of new information. Why do misconceptions survive in some groups, given that people are exposed to high-quality information (Gentzkow and Shapiro (2011); Guess et al. (2018))? We offer a simple explanation, complementing recent models that instead highlight the role of social media echo chambers (Bowen et al. (2021)): Within a community or ideological bubble, people are exposed to crowdsourced models that evolve to better and better fit data that is open to interpretation, making them less persuadable. In our framework, bubbles do not prevent people from being exposed to the right interpretation of an event, but they inoculate against finding that interpretation compelling. Such inoculation may shed light on why reducing exposure to like-minded information on social media does not appear to significantly impact beliefs (e.g., Nyhan et al. (2023)).

#### **Related Literature**

There is a large literature on social learning reviewed in Golub and Sadler (2016), with influential early contributions in economics such as Banerjee (1992), Bikhchandani et al. (1992), and Smith and Sørensen (2000). While much of this work assumes Bayesian updating of beliefs, important recent contributions study naive social learning by building on the simple DeGroot (1974) model of linear updating (Golub and Jackson (2010)) or on psychologically microfounded updating rules (e.g., Eyster and Rabin (2010, 2014); Enke and Zimmermann (2019); DeMarzo et al. (2003); Gagnon-Bartsch and Rabin (2016)). This work focuses on people sharing information or observing each others' actions, and studies questions like whether social learning successfully aggregates individuals' private information. Our focus is instead on the many situations where people share essentially the same information, and social learning primarily involves exchanging interpretations to make sense of that information.

While social learning of information tends to predict long-run consensus and relatively effective information aggregation, in our framework the marketplace for models generates long-run disagreement and the persistence of false beliefs. As such, it may help explain why disagreement persists in domains from stock prices to public health to evolution, despite an abundance of data. Increasing connectedness tends to unterher beliefs from data that is open to interpretation by increasing the chances of being exposed to a model that provides a compelling case that the data is unsurprising. Wrong interpretations are adopted in our framework not because they are repeatedly heard, but because social learning selects interpretations that compellingly fit people's prior knowledge.

A smaller literature on social learning examines how people could leverage networks to their advantage in spreading information. Much of this work considers how to best seed a network with information to boost its diffusion (e.g., Akbarpour et al. (2020)). Murphy and Shleifer (2004) present a model of the creation of social networks based on shared beliefs in the context of political persuasion. This work considers social learning of information or beliefs rather than of models.

Closer to our work, recent presidential addresses in finance, such as Shiller (2017) and Hirshleifer (2020), have called for studying the social transmission of narratives in economics.<sup>5</sup> These addresses laid the groundwork for this study by providing vivid illustra-

<sup>&</sup>lt;sup>5</sup>While not all narratives are models and vice versa, they are closely related and we sometimes inter-

tions of the importance of socially-emergent narratives as drivers of economic and financial events. They also sketch models of narrative transmission that liken the spread of narratives to the spread of viruses. Bénabou et al. (2018) model the spread of moral narratives (e.g., "thou shall not do this because") by strategic actors, while Bursztyn et al. (2023) and Bursztyn et al. (2022) argue that providing rationales and narratives importantly influences people's willingness to voice certain beliefs. Our work adds to this area by formally model-ing social forces that shape the narratives themselves and highlighting that high explanatory power helps narratives "go viral".

We build on our earlier work on model persuasion (Schwartzstein and Sunderam (2021)), which itself built on behavioral models of persuasion based on coarse or associational thinking (e.g., Mullainathan et al. (2008)).<sup>6</sup> Froeb et al. (2016) present an earlier related model in the context of studying adversarial decision making in law, Levy and Razin (2020) present a related model speaking to the problem of combining expert forecasts, Aina (2021) builds on the model persuasion framework by considering what happens when persuaders need to commit to models before seeing all the data, and Ichihashi and Meng (2021) considers the interaction between Bayesian persuasion (Kamenica and Gentzkow (2011)) and model persuasion. Other recent work (Eliaz and Spiegler (2020); Bénabou et al. (2018); Yang (2022); Eliaz et al. (2022)) take somewhat different approaches to formalizing models or narratives and what makes them persuasive. For example, Eliaz and Spiegler (2020) assume that people favor "hopeful narratives", Eliaz et al. (2022) assume that narratives emerge competitively to increase political mobilization, and Yang (2022) assumes that people favor "decisive models". A growing empirical and experimental literature measures people's models or narratives, as well as how they influence expectations and decisions (e.g., Barron and Fries (2022); Andre et al. (2022); Flynn and Sastry (2022); Hüning et al. (2022)). We add to this work by formalizing how social learning influences which models emerge and persist.

changeably use the terms narratives, stories, and models.

<sup>&</sup>lt;sup>6</sup>Our framework also connects to the literature on learning under misspecified models (e.g., Esponda and Pouzo (2016); Acemoglu et al. (2016); Heidhues et al. (2018); Montiel Olea et al. (2022); Mailath and Samuelson (2020); Haghtalab et al. (2021)), which sometimes feature agents who statistically test their models and abandon them in favor of alternatives which fit better. Examples include Fudenberg and Kreps (1994); Hong et al. (2007); Gagnon-Bartsch et al. (2021); Fudenberg and Lanzani (2021); Ba (2021).

### 2 Model

#### 2.1 Setup

The basic setup follows Schwartzstein and Sunderam (2021). Broadly, individual agents take the following steps. All agents have a common default model for interpreting data; each agent also comes up with a model of their own. Prior to social learning, each agent selects from these two models the one that best explains the data. Social learning then exposes each agent to all models held by other agents in her community. After social learning, each agent adopts the model that best explains the data from the set of models she has been exposed to: the default, the model she comes up with on their own, and the models others in her community have come up with.

Formally, there is a continuum of agents  $i \in [0, 1]$  who hold beliefs  $\mu_i$  over states of the world  $\omega$  in finite set  $\Omega$ .<sup>7</sup> Agent *i* takes an action *a* from compact set *A* to maximize the expectation under  $\mu_i$  of  $U_i(a, \omega)$ . In the baseline setup, agents share a common prior  $\mu_0 \in \operatorname{int}(\Delta(\Omega))$  over  $\Omega$  and observe a public history of past outcomes, *h*, drawn from finite outcome space *H*. Agents can end up with different posteriors if they use different models to interpret this history. Given state  $\omega$ , the likelihood of *h* is given by  $\pi(\cdot|\omega)$ . The true model  $m^T$  is the likelihood function  $\{\pi_{m^T}(\cdot|\omega)\}_{\omega\in\Omega} = \{\pi(\cdot|\omega)\}_{\omega\in\Omega}$ . We assume that every history  $h \in H$  has positive probability given the prior and true model.

Agents do not know the true model. A given agent updates her beliefs based on either (i) the default model  $\{\pi_d(\cdot|\omega)\}_{\omega\in\Omega}$ ,<sup>8</sup> (ii) the model  $m'_i$  that she generates herself to explain the history, where  $m'_i$  is taken from compact set M and indexes a likelihood function  $\{\pi_{m'_i}(\cdot|\omega)\}_{\omega\in\Omega}$ , or (iii) a model she learns from someone in her community, where we let  $M_i \subseteq M$  denote the set of models proposed by someone in *i*'s community.

Given the history and the set of models the agent is exposed to, she adopts the one that best explains the history. Formally, let  $\mu(h, \tilde{m})$  denote the posterior distribution over  $\Omega$  given h and model  $\tilde{m} \in M \cup \{d\}$ , as derived by Bayes' rule. We assume the receiver adopts the model m and hence posterior  $\mu(h, m)$  if

$$m \in \arg \max_{\tilde{m} \in \{d, m'_i\} \cup M_i} \underbrace{\Pr(h|\tilde{m}, \mu_0)}_{= \int \pi_{\tilde{m}}(h|\omega)d\mu_0(\omega)}.$$

<sup>&</sup>lt;sup>7</sup>In examples we sometimes relax the assumption that  $\Omega$  is finite.

<sup>&</sup>lt;sup>8</sup>The default can be a function of h. We suppress this dependence when it does not cause confusion.

That is, the person picks the model she is exposed to that best fits the data. Upon adopting a model  $\tilde{m}$ , the person uses Bayes' rule to form posterior  $\mu(h, \tilde{m})$  and takes an action that maximizes her expected utility given that posterior belief:  $a(h, \tilde{m}) \in \arg \max_{a \in A} \mathbb{E}_{\mu(h, \tilde{m})}[U_i(a, \omega)]$ .

To close the baseline model, we need to specify the model a person generates herself. Let  $\overline{M}(h, \mu_0, d, M) = \{m \in M : \Pr(h|m, \mu_0) \ge \Pr(h|d, \mu_0)\}$  denote the set of models in M that explain the history as well as the person's default interpretation given her prior over states. Assume that measure  $\delta$  of the population generates the default model and measure  $(1 - \delta)$  generates a model in  $\overline{M}(h, \mu_0, d, M)$ .<sup>9</sup> Further assume that population is large enough that, for each model  $m \in \overline{M}(h, \mu_0, d, M)$ , someone in the population generates that model herself.

In the typical case, we set the default interpretation to be the true model,  $d = m^T$ and focus on situations where data are open to interpretation—i.e., where people are in fact sharing interpretations of data. We also often let M be the set of all possible models  $M^a$ : for any likelihood function  $\{\tilde{\pi}(\cdot|\omega)\}_{\omega\in\Omega}$  there is an  $m \in M^a$  with  $\{\pi_m(\cdot|\omega)\}_{\omega\in\Omega} =$  $\{\tilde{\pi}(\cdot|\omega)\}_{\omega\in\Omega}$ . We refer to this as the case where people are *maximally open to persuasion*. We simply write  $\bar{M}(h, \mu_0)$  as shorthand for  $\bar{M}(h, \mu_0, m^T, M^a)$ .<sup>10</sup>

### 2.2 Discussion of Model Assumptions

The building blocks of the model come from Schwartzstein and Sunderam (2021), and we refer to that paper for a detailed discussion of the basic assumptions. We depart from that paper in a few crucial ways. First, we allow some receivers by themselves to generate a model other than the default. In the notation of our current framework, our previous paper assumes  $\delta = 1$  (receivers stick with the default before being exposed to persuasion), while this paper focuses on the case where  $\delta < 1$ . For many topics, it is plausible that some people generate an initial interpretation of the data, prior to sharing interpretations with others. Many of us have gut reactions about why the stock market moved yesterday,

<sup>&</sup>lt;sup>9</sup>Alternatively, we could endogenize  $\delta$  by assuming that people sometimes generate models outside of  $\overline{M}(h, \mu_0, d, M)$  in which case they stick with the default model. This would suggest that  $\delta$  is larger when the default does a good job explaining the data h. While this change would influence the distribution of beliefs prior to social learning, it would not influence the distribution of beliefs following social learning.

<sup>&</sup>lt;sup>10</sup>All our results and intuitions stated for the case of  $M = M^a$  continue to hold if we instead make the following assumption on M: For every belief  $\tilde{\mu}$  that is a posterior for some model in  $M^a$  given data h, prior  $\mu_0$ , and default d, M includes the best-fitting model inducing that posterior as well as one worse-fitting model inducing that posterior.

who is responsible for the storming of a government building, or what the latest school shooting implies about the merits of gun control. These gut reactions may be constructed spontaneously in response to the data and differ across people (see, e.g., Andre et al. (2022) for evidence of heterogeneity in households' and experts' models of the causes of inflation). Crucially, however, we assume that a given person does not come up with all models she is willing to entertain, so she is influenced by the set of models she is exposed to.

Second, this paper's analysis focuses on the social exchange of models, not on the behavior of a strategic persuader who attempts to influence a receiver. The role of the community or network in our framework is simply to influence the set of models a person is exposed to. By taking as primitive the set of models a given person i is exposed to,  $M_i$ , our framework accommodates a variety of community structures.

Third, implicit in the idea that a person is exposed only to the models within her community is an assumption that she does not actively seek out the models proposed by members of other communities. One way of thinking about this assumption is that people exhibit a sort of out-group homogeneity bias (e.g., Quattrone and Jones (1980); Bursztyn and Yang (2023)), thinking there is not much reason to investigate the models in other communities because they are "all the same". A person who favors gun control may be aware of some arguments for why shootings suggest weaker gun control (e.g., "we need more guns in the hands of good guys") and may think once she has heard one such argument she has heard them all, perhaps underappreciating the diversity of these arguments.

### 2.3 Examples

We now sketch two brief examples, which we will return to throughout the paper.

**Example 1** (Interpreting data about investments). Extend the example from the introduction to the following *multiple dimension* setup: let  $h = (h_1, h_2, ..., h_N)$  with  $h_j \in H_j$ ,  $H_j$  finite, for each j = 1, 2, ..., N. For example,  $h_1$  could stand for whether the aggregate economy has entered a recession,  $h_2$  for whether company earnings are high or low, and  $\omega$  for whether company fundamentals are good or bad. Let  $\pi_j(h_j) \equiv \sum_{\omega'} \pi_{m^T,j}(h_j|\omega') \cdot \mu_0(\omega')$ denote the true marginal probability of  $h_j$  for each j, where each marginal probability  $\pi_{m,j}(h_j|\omega)$  is derived from  $\pi_m(h|\omega)$  in the obvious way. Suppose that, as in the introductory example, the set of models agents are willing to entertain agree with  $\pi_{m^T}(h|\omega)$  on these marginal probabilities:

$$M = \left\{ m \left| \sum_{\omega'} \pi_{m,k}(h_k | \omega') \cdot \mu_0(\omega') = \pi_k(h_k) \ \forall h_k, \ k \in \{1, 2, \dots, N\} \right\} \right\}.$$

**Example 2** (Interpreting data about policy issues). Our second example involves interpreting data about a binary state space,  $\Omega = \{l, r\}$ . Unlike the first example, here the space of models is unrestricted. The prior over states is  $\mu_0(l) = 1/2$ . Further assume people are maximally open to persuasion,  $M = M^a$ , and the default model is the true model,  $d = m^T$ . People can take three possible actions,  $a \in \{L, M, R\}$ . Payoffs  $U_i$  are such that the optimal action is a = L if  $\mu(l) \ge .75$ , a = M if  $\mu(l) \in (.25, .75)$ , and a = R if  $\mu(l) \le .25$ .

This example can capture optimal public-policy choices. In state  $\omega = l$ , a Democrat would make a better US president, and in state  $\omega = r$  a Republican would make a better US president. Actions correspond to voting Democrat (a = L), abstaining (a = M), and voting Republican (a = R). Alternatively, one can think of the states as corresponding to whether some left- or right-leaning policy (e.g., involving gun control, climate change, pandemic policy) would be effective, and the actions as corresponding to supporting such policies (a = L, R) or the status quo (a = M). The example can also capture choices of firms, for instance to cut costs, grow, or stay the course.

We will sometimes extend this example to cases where people may use the same data to update beliefs about a variety of issues. For instance, people may interpret data about genetically-modified crops using models that have implications for both their safety and impact on the environment (e.g., how their adoption influences pesticide use). To accommodate such examples, let  $\Omega = \Omega^1 \times \Omega^2$ . We will consider how community members' beliefs over  $\Omega^1$  spill over to influence beliefs over  $\Omega^2$ .

### 2.4 Basic Observations and Definitions

Prior to social learning, a person adopts the model

$$m' \in \arg\max_{\tilde{m} \in \{d, m'_i\}} \Pr(h|\tilde{m}, \mu_0)$$

and holds beliefs  $\mu(h, m')$ , which we call their "initial reaction."

Appendix Section B.1 analyzes initial reactions before social learning, adapting Propo-

sition 1 in Schwartzstein and Sunderam (2021) to the present context. Two key points follow. First, before social learning, people have a variety of reactions to the data. Second, there are constraints on initial reactions, which in turn imply constraints on final beliefs. In particular, the set of initial reactions is constrained by prior beliefs,  $\mu_0(\omega)$ , as well as the ability of the default to explain the data given those prior beliefs,  $\Pr(h|d, \mu_0)$ . Intuitively, the better the default model fits the data, the harder it is for an initial reaction to fit the data even better. And the more unlikely a state under peoples' prior, the less likely it is that their beliefs following their initial reaction put a lot of weight on that state. If the data is maximally open to interpretation, sticking with prior beliefs is always an initial reaction to the data and the range of initial reactions is greater when people are more surprised by the data, i.e., when  $\Pr(h|d, \mu_0)$  is lower.<sup>11</sup>

Following social learning, the person adopts the model

$$m \in \arg \max_{\tilde{m} \in \{d, m'_i\} \cup M_i} \Pr(h|\tilde{m}, \mu_0)$$

and holds beliefs  $\mu(h, m)$  when such maximizers exist—assume throughout the paper that  $M_i$  is indeed such that such maximizers exist. As shorthand, write  $\mu'_i(m'_i)$  as person *i*'s beliefs (adopted model) prior to social learning and  $\mu_i(m_i)$  as her beliefs (adopted model) following social learning.

We say that social learning *hardens* a person's reaction to data when she can better explain the data following social learning than before: that is, when  $\Pr(h|m_i, \mu_0) \ge \Pr(h|m'_i, \mu_0)$ . When social learning does not harden the person's reaction, we say it *softens* her reaction. We say that social learning *mutes* a person's reaction to data when it moves her beliefs closer to her prior. Formally, following Schwartzstein and Sunderam (2021), let  $\operatorname{Movement}(\tilde{\mu}; \mu_0) \equiv \max_{\omega \in \Omega} \tilde{\mu}(\omega)/\mu_0(\omega)$  be a measure of the change in beliefs from prior  $\mu_0$  to posterior  $\tilde{\mu}$ . Social learning mutes reactions to the data when  $\operatorname{Movement}(\mu_i; \mu_0) \leq \operatorname{Movement}(\mu'_i; \mu_0)$ . When social learning does not mute a person's reaction to data, we say it *intensifies* her reaction. Note that these terms compare final beliefs to people's initial reactions to data before social learning, not to their prior.

A simple observation is that our assumptions imply that social learning must harden reactions to data: being exposed to more explanations of the data enables the person to

<sup>&</sup>lt;sup>11</sup>The range of initial reactions will be smaller when prior beliefs are more informed, e.g., because they reflect a long history of closed-to-interpretation data (see Proposition 2 in Schwartzstein and Sunderam (2021)).

better explain the data. Social learning leads a person to become more convinced she understands why the market moved as it did, why an unexpected political event occurred, or the daily movement in pandemic deaths. Following social learning, any event seems more explainable.

## **3** Social Exchange of Models

### 3.1 Shared-Belief Communities

In our framework, the community determines the set of models that people are exposed to. Community formation therefore plays a crucial role in determining ultimate beliefs. Throughout the paper, we will frequently analyze the case where communities are formed on the basis of shared beliefs. Such communities are quite common (e.g., McPherson et al. (2001)). For instance, communities are formed based on political beliefs, views on vaccines, and even whether a specific stock is likely to rise (Cookson et al. (2022)). Social media has facilitated the formation of such communities and the exchange of interpretations among their members. Of course, communities may also form for other reasons, such as geographical proximity or shared models. We briefly discuss implications of alternative community structures in Section 7.

The key feature of a *shared-belief community* is that the beliefs a person holds prior to talking to others influences who she talks to. Formally, consider a partition S over the set of beliefs  $\Delta(\Omega)$ , where we denote  $s(\mu)$  as the element in S that belief  $\mu \in \Delta(\Omega)$  belongs in. In a shared-belief community, a person *i* exchanges models with another person *j* if and only if their initial beliefs are similar, in the sense that they fall in the same element of S.

**Definition 1.** In a shared-belief community,  $M_i = \{m \in \overline{M}(h, \mu_0, d, M) : \mu(h, m) \in s(\mu(h, m'_i))\}$  for every person *i*.

Given our assumption of common priors, this definition says that a shared-belief community forms based on a common reaction to a specific event. For example, a shared-belief community could form among people who react similarly to a shooting in their beliefs on the need for gun control. This literal interpretation is a reasonable approximation of reality for certain events, such as the earnings announcements we consider in Section 3.2. However, in other instances communities based on shared beliefs are grounded in common reactions to a broader set of events. For example, people who lean left in their interpretations might share views on the most recent event, even if their initial views on that most recent event are quite different. We will more formally capture this idea in briefly studying dynamics in Section 6.

To illustrate, consider a complete network and return to Example 1.

**Proposition 1.** In the multiple dimension setup (described in Example 1), suppose  $\tilde{h} = (\tilde{h}_1, \tilde{h}_2, \ldots, \tilde{h}_N)$  is realized, where (without loss of generality)  $\pi_1(\tilde{h}_1) \leq \min_{k>1} \pi_k(\tilde{h}_k)$ . Even if the relationship between each variable k > 1 and variable j = 1 is  $\Pr(\tilde{h}_k | \tilde{h}_1, m^T, \mu_0) - \Pr(\tilde{h}_k | m^T, \mu_0) = 0$ , social learning in a complete network leads people to hold a model  $m' \in M$  that maximally connects the variables: For all k,

$$\Pr(\tilde{h}_k|\tilde{h}_1, m', \mu_0) - \Pr(\tilde{h}_k|m', \mu_0) = \max_{m \in M} \Pr(\tilde{h}_k|\tilde{h}_1, m, \mu_0) - \Pr(\tilde{h}_k|m, \mu_0) = 1 - \pi_k(\tilde{h}_k).$$

Under any such model m' that has the property that  $\pi_{m'}(\tilde{h}_1|\omega)$  is constant across values of  $\omega$ , people's posterior beliefs equal their prior beliefs  $\mu_0$ .

Proof. All proofs are in Appendix A.

As in the introductory example, natural restrictions on the model space clarify how social learning may lead people to draw connections between events that they would otherwise be surprised by. The proposition shows that people end up holding models that view the rarest realized  $h_i$  as implying all the more common realized  $h_j$ 's with certainty. For example, when recessions are rarer than low earnings, low earnings are viewed as being inevitable given recessions. When high earnings are viewed as more likely than a good economy, then high earnings are viewed as inevitable given a good economy, and a bad economy is viewed as unsurprising given low earnings. Put differently, people have a tendency to say "of course X (more common outcome) given Y (rarer outcome)". Explanations and sense-making center around the rarest outcome. Thus, our framework puts structure on the kinds of "conspiratorial" links that groups of people will tend to draw between unrelated events. Models drawing these links in a sense simplify the world by viewing a single root cause (e.g., recessions) as responsible for a variety of outcomes (e.g., low earnings). The proposition additionally shows that such explanations neutralize the data, leaving posterior beliefs the same as prior beliefs, so long as people do not view the rare outcome as itself signaling something about  $\omega$ , e.g., they do not think a recession by itself provides news about whether a company is good.

Neutralization of the data is in fact the norm if people are maximally open to persuasion. We first recall a lemma from Schwartzstein and Sunderam (2021).

Lemma 1 (Schwartzstein and Sunderam (2021)). Fix history h and let

$$Fit(\tilde{\mu}; h, \mu_0) \equiv \max_m \Pr(h|m, \mu_0)$$
 such that  $\mu(h, m) = \tilde{\mu}$ 

be the maximal fit of any model that induces posterior  $\tilde{\mu}$  given the history h and a person's prior  $\mu_0$ . Then

$$Fit(\tilde{\mu}; h, \mu_0) = 1/Movement(\tilde{\mu}; \mu_0),$$

where  $Movement(\tilde{\mu}; \mu_0) \equiv \max_{\omega \in \Omega} \tilde{\mu}(\omega) / \mu_0(\omega)$  is the movement to  $\tilde{\mu}$  from  $\mu_0$ .

Intuitively, fit and movement are inversely related because models that fit the history well say it is unsurprising in hindsight, which then implies that beliefs should move little. So, for any given belief  $\mu$ , the maximal fit of a model inducing that belief is greater the closer this belief is to  $\mu_0$ .

**Proposition 2.** Suppose everyone is in a shared-belief community and is maximally open to persuasion,  $M = M^a$ . Then social learning mutes every person's reaction to the data: for every person i,  $Movement(\mu_i; \mu_0) \leq Movement(\mu'_i; \mu_0)$ . In fact, social learning leads everyone's final beliefs to be in the set of initial beliefs within the community that are closest to the prior: for every person i,  $\mu_i \in \arg \min_{\mu \in s(\mu'_i)} Movement(\mu; \mu_0)$ .

This result says that if a person only exchanges models with others who react similarly to data, they end up with the belief that reacts least to the data *within their community*. This result follows from Lemma 1 and the following feature of shared-belief communities: For every belief represented in a community, the best-fitting model supporting that belief is represented in the community.

As an illustration, suppose that in the public-policy example (Ex. 2),  $\mu_0(l) = 1/2$ and the data is surprising—i.e., under the default model, it has very low probability. For example, suppose h = "a natural disaster struck and GDP growth this quarter was low." Suppose further that shared-belief communities are formed based on views of the optimal action: Everyone with an initial reaction supporting a right-leaning action like a tax cut is in one community  $(\mu'_j(l) \in [0, 1 - k])$  for  $k \in (.5, 1)$ ), everyone with an initial reaction supporting the neutral action is in another  $(\mu'_j(l) \in (1 - k, k))$ , and everyone with an initial reaction supporting a left-leaning action like stimulus checks is in the third community  $(\mu'_j(l) \in [k, 1])$ . The variable k could be viewed as parameterizing the degree to which people form shared-belief communities based on the intensity of their views on the issue. Under this interpretation, it is larger when people connect with others based on their views about the issue (e.g., through social media) and smaller when people connect with others for other reasons (e.g., because they live in the same physical neighborhood).

Proposition 2 says that everyone ends up at the belief that is closest to the prior within her community (Figure 1 illustrates this for k = .75). For example, someone whose initial reaction to the data moves her belief from  $\mu_0(l) = .5$  to  $\mu'(l) = .9$  will exchange models with others whose initial reactions support the left-leaning action (pictured in blue in the figure), which mutes her reaction to  $\mu(l) = k$ . Polarization in views across the left- and right-leaning communities equals k - (1 - k) = 2k - 1: it is increasing in the extent to which people talk to others based on their views along the issue. In other words, the community formation process (indexed by k) drives polarization across communities, while the exchange of models drives the homogeneity of beliefs within the community.<sup>12</sup>

To further illustrate Proposition 2, a school shooting might initially lead people to support a change in gun-control policies, but they will eventually favor interpretations that say we did not learn much from the shooting. Empirical evidence suggests such dynamics. Following mass shootings, Twitter users who are initially against gun control temporarily become more open to it. However, as narratives evolve, these Twitter users slowly revert back towards their original beliefs (Lin and Chung (2020)).

Taken together, these results highlight the differences between our framework and typical information-based theories of social learning, in which social exchanges of information tend to lead to more accurate beliefs. In our setting, social exchanges of models increase the chances of hearing an interpretation that suggests the data are relatively consistent with a person's prior and hence there is little need to update. In other words, the "marketplace of ideas" need not result in beliefs that are closer to the truth.

<sup>&</sup>lt;sup>12</sup>Appendix C provides an example that shows how interpretations may evolve differently across sharedbelief communities, illustrating an additional form of polarization.

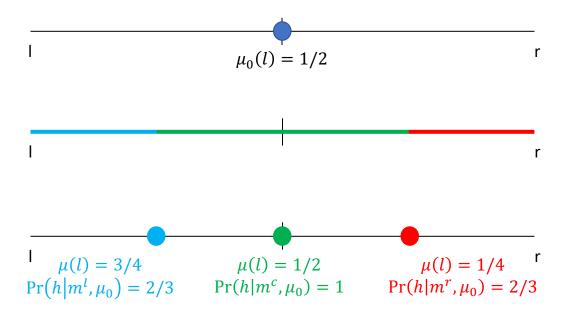


Figure 1: Evolution of Beliefs Across Shared-Belief Communities

#### **3.2 Empirical Evidence**

We next provide evidence consistent with Proposition 2. We use data from StockTwits, an online social media platform for investors that has been studied in recent papers, including Cookson and Niessner (2020), Divernois and Filipovic (2022), and Cookson et al. (2022). StockTwits is similar to Twitter: users choose other users to follow and post short messages visible to their followers. Founded in 2008, the platform had 6 million total users and 1 million active monthly users at the end of 2021.<sup>13</sup> The platform is geared towards allowing investors to share with each other information and analysis about individual stocks. In particular, it allows users to (i) tag their messages with individual stock tickers and (ii) label their messages with a flag for optimistic ("bullish") or pessimistic ("bearish") sentiment. These features make it straightforward to track a particular user's sentiment towards a particular stock over time. Cookson and Niessner (2020) perform a variety of exercises to validate the data's quality for measuring sentiment and disagreement.

Two stylized facts from StockTwits are relevant to our framework. First, based on the evidence in Cookson et al. (2022), the way we model the formation of a shared-belief community is consistent with how StockTwits members actually form their communities.

<sup>&</sup>lt;sup>13</sup>See this (link) Bloomberg article.

Cookson et al. (2022) show that users who are bullish on a particular stock are more likely to start following other users who are also bullish on the same stock. Similarly, bearish users are more likely to start following other bearish users. Moreover, this behavior is more pronounced immediately following earnings announcements. In other words, following a news announcement, StockTwits users are more likely to form communities with others who share their views on a particular stock.

Second, beliefs of StockTwits users around earnings announcements evolve as Proposition 2 predicts. We analyze the dynamics of user sentiment around earnings announcements in StockTwits messages between January 2011 and July 2018.<sup>14</sup> Users label their messages as bullish (coded as 1) or bearish (0). We analyze 20-day windows surrounding each earnings announcement, restricting attention to users who have ever posted a message about that stock prior to 10 days before the earnings announcement. Users are coded as a bull on the stock if they labeled as bullish at least 50% of their messages about the stock prior to 10 days before the earnings announcements. We then track how sentiment evolves around earnings announcements. An announcement is positive news if the announcement day return is greater or equal to zero and negative news otherwise. Because different stocks receive different amounts of attention, we weight the data so that each earnings announcement is equally weighted. The final sample consists of roughly 1.8 million messages across 40,000 earnings announcements from 65,000 unique users.<sup>15</sup>

Figure 2a shows the evolution of sentiment for bulls around positive and negative earnings announcements with 95% confidence intervals. Corresponding regressions are reported in Appendix D. The figure shows that around positive announcements, bulls' sentiment remains unchanged: generally 94-95% of messages are labeled as bullish. The pattern around negative earnings announcements contrasts sharply. Sentiment deteriorates in the days leading up to the earnings announcement. There is then a sharp decline in sentiment at the earnings announcement, with the fraction of messages labeled as bullish falling to

<sup>&</sup>lt;sup>14</sup>We thank Marc-Aurèle Divernois and Damir Filipović for very generously sharing their data with us. Divernois and Filipovic (2022) study this data, showing that sentiment measured from StockTwits can be used to forecast stock returns on high-message volume days.

<sup>&</sup>lt;sup>15</sup>The sample is smaller than the overall scale of StockTwits for several reasons. First, we focus on messages about individual stocks, not indices like the S&P 500. Second, we restrict to attention to messages labeled as bullish or bearish by users. Third, we focus on windows around earnings announcements, which account for less than one-third of trading days. Finally, the requirement that the user has posted a message with a bullish/bearish label about the stock prior to the earnings announcement is restrictive.

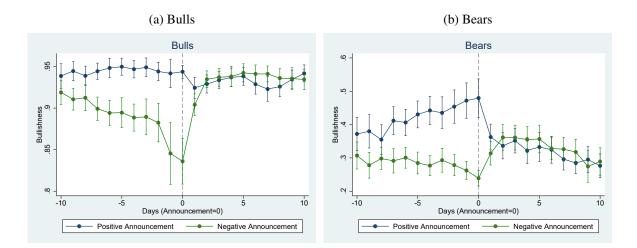


Figure 2: Evolution of Beliefs Around Earnings Announcements

under 85%, statistically and economically different from its baseline value.<sup>16</sup> In the days following the announcement, however, sentiment rapidly improves, converging back to 94-95% bullish. Within two days of the announcement, sentiment is the same, regardless of whether the announcement was positive or negative news. Figure 2b shows similar patterns for bears around positive news announcements. Sentiment first improves but then reverts.

These patterns are consistent with our theoretical results.<sup>17</sup> Following a news announcement, users form communities with users of similar beliefs. Within those communities, they are exposed to interpretations of the data that make it less surprising. Thus, while users' initial reactions may push them away from their prior beliefs, the community will expose them to interpretations of the data that pull them back. Bulls about a stock become more bearish following a negative announcement, for example, but they return to being bullish once they are exposed to the best-fitting interpretations that evolve within the bullish community.

However, a key question remains: How do bulls and bears persistently disagree when bulls are likely exposed to at least *some* of the arguments of bears and vice-versa? The next

<sup>&</sup>lt;sup>16</sup>Average sentiment for bulls during these event windows is 0.94 with a standard deviation of 0.24. For bears, the corresponding numbers are 0.28 and 0.45.

<sup>&</sup>lt;sup>17</sup>Our data do not allow us to directly demonstrate that these patterns are driven by the community—they could reflect evolving interpretations people come up with by themselves. However, in traditional social learning models based on sharing information, the community should push against such tendencies.

section takes up this question.

# 4 Communication Across Communities and Issues

### 4.1 Communication Across Communities

Can inaccurate beliefs and disagreement persist as people communicate across communities and issues? We first consider the impact of two different types of communication across communities. We show that differences in beliefs can persist when members of one community only hear some arguments made by members of another community. In other words, ideological bubbles need not be hermetically sealed. So long as only some arguments are transmitted across communities, differences in beliefs can persist.

Person *i* is weakly exposed to belief  $\tilde{\mu}$  if the set of models she is exposed to expands from  $M_i$  to  $M_i \cup \{m(\tilde{\mu})\}$ , where  $m(\tilde{\mu})$  is a specific model that supports belief  $\tilde{\mu}$ . On the other hand, a person is strongly exposed to belief  $\tilde{\mu}$  if the set of models she is exposed to expands from  $M_i$  to  $M_i \cup M(\tilde{\mu})$ , where  $M(\tilde{\mu})$  is the set of all models that induce  $\tilde{\mu}$ . A person is exposed to belief  $\tilde{\mu}$  if she is either weakly or strongly exposed to  $\tilde{\mu}$ . We think of weak exposure as capturing most communication across communities. For instance, a person who views evidence as suggesting that a new vaccine is safe is likely aware that there are people in "anti-vaccine" communities who believe otherwise. However, this person is likely only aware of a thin slice of anti-vaccine arguments.

We say a person is *persuaded* through exposure to belief  $\tilde{\mu}$  if such exposure changes her final beliefs. Person *i* is more persuadable than person *j* if *i* is persuaded through exposure to belief  $\tilde{\mu}$  whenever *j* is.

**Proposition 3.** Suppose everyone is maximally open to persuasion,  $M = M^a$ .

- Suppose person i is weakly exposed to a belief μ not represented in her community. Independent of her community and the alternative belief, the person need not be persuaded through this exposure: For every set of models M<sub>i</sub> and belief μ not supported by any model in M<sub>i</sub>, there exists positive measure of models m̃ = m(μ̃) supporting μ that fit less well than the best-fitting model in M<sub>i</sub>.
- 2. Suppose person *i* is strongly exposed to a belief  $\tilde{\mu}$  not represented in her community.

Then the person is persuaded by this exposure if  $\tilde{\mu}$  is closer to her prior, as measured by Movement( $\cdot; \mu_0$ ), than any belief supported by a model in  $M_i$ .

The first part of Proposition 3 implies that weak exposure to beliefs outside a person's community is never guaranteed to impact her beliefs. The second part implies that strong exposure to an alternative belief has at least as much impact on ultimate beliefs and behavior as weak exposure. While weak exposure to an alternative belief is never guaranteed to move final beliefs, strong exposure will move final beliefs whenever the alternative belief is closer to the person's prior than other beliefs represented in her community.

These results help explain why different beliefs persist across communities, such as StockTwits, even though there is communication across communities. We think of crosscommunity communication as weak exposure. People might exchange both models and beliefs when interacting with others in the same community, while only exchanging beliefs (and perhaps a subset of models supporting those beliefs) when interacting with members of different communities. For instance, a person who believes a school shooting indicates the need for stricter gun-control measures is likely aware that there are others who conclude the opposite without being intimately familiar with all of their arguments. Proposition 3 says that weak exposure to anti-gun control arguments need not move the beliefs in the pro-gun control community. While a person could become convinced by listening to a broad set of arguments for a position, she is less likely to be convinced by a narrow subset of the arguments (or simply a statement of the position itself).<sup>18</sup> This result highlights a key difference between our framework and information-based approaches. In informationbased approaches, if two communities start from the same prior and see the same data, they will end up with the same beliefs. In contrast, in our setting only strong exposure will tend to lead to convergence in beliefs.

### 4.2 Communication Across Issues

Of course, new communities do not form around every issue, even in the age of social media. Often, a community formed on one issue starts discussing a second. For instance, a

<sup>&</sup>lt;sup>18</sup>In highlighting the importance of the breadth of arguments a person is exposed to, our model relates to "persuasive-arguments theory" from psychology (e.g., Burnstein and Vinokur (1977) and Hüning et al. (2022)). However, persuasive-arguments theory emphasizes the number of distinct arguments a person is exposed to, while we emphasize the compellingness of arguments (in terms of fit).

group of vaccine skeptics might also discuss the merits of public education. In this subsection, we consider how communities formed on shared beliefs about one issue influence beliefs on a second issue. We show that Proposition 2 has implications for *cross-issue* polarization.

Formally, consider an extension of the policy example where there are two issues:  $\Omega = \Omega^1 \times \Omega^2$  and describe marginal beliefs over  $\Omega^j$  by  $\mu^j$ . For concreteness, let  $\Omega^1 = \{l, r\}$  be whether a left- or right-leaning candidate governs better and  $\Omega^2 = \{n, y\}$  be whether the economy will grow next quarter (y) or not (n). Communities are formed based on initial beliefs over  $\{l, r\}$  but not  $\{n, y\}$ :  $s(\mu)$  depends only on  $\mu^{1'}$ . Suppose that  $\Omega^1$  and  $\Omega^2$  are binary, with priors given by the following table:

$\mu_0$	n	y
l	a	b
r	b	a

Suppose further that  $\mu_0(l) = .5$  and, for  $k \ge \mu_0(l)$ , shared belief communities are formed based on whether  $\mu^{1'}(l) \ge k$  (the left-leaning community),  $\mu^{1'}(l) \in (1 - k, k)$  (the centrist community), and  $\mu^{1'}(l) \le 1 - k$  (the right-leaning community). Refer to this generalization of the multiple-issues policy example as the *multiple issues setup*.

**Corollary 1.** In the multiple issues setup, shared-belief communities of intensity  $k \ge \mu_0(l)/(\mu_0(l) + \mu_0(l, y))$  formed based on views on issue l versus r spill over to influence views of issue y versus n: The simple average between the lowest and highest potential values of  $\mu_i^{\text{left-leaning}}(y) - \mu_j^{\text{right-leaning}}(y)$  across people i (in the left-leaning community) and j (in the right-leaning community) equals

$$\begin{cases} \frac{1}{2} \times k \times (\mu_0(y|l) - \mu_0(y|r) + 3) - 1 & \text{if } k < \frac{\mu_0(l)}{\mu_0(l) + \mu_0(r,y)} \\ k \times (\mu_0(y|l) - \mu_0(y|r)) & \text{if } k \ge \frac{\mu_0(l)}{\mu_0(l) + \mu_0(r,y)} \end{cases}.$$

$$\tag{1}$$

Moreover, for  $k \geq \frac{1}{2 \times \mu_0(y|l)}$ , the lower bound of  $\mu_i^{left-leaning}(y) - \mu_j^{right-leaning}(y)$  is greater than 0 when  $\mu_0(y|l) > \mu_0(y|r)$ .

Even though beliefs over the second issue do not influence community formation, final beliefs over that issue differ across members of the left-leaning and right-leaning communities. Corollary 1 (of Proposition 2) identifies two factors that influence belief polarization in views about y versus n, given by Equation (1). First, polarization is increasing in

k, which could be interpreted as the degree to which communities are formed based on shared beliefs along issue l versus r—e.g., the extent to which people connect with others because of their views about that issue. Second, such polarization is increasing in the degree  $(\mu_0(y|l) - \mu_0(y|r))$  to which issue y versus n is prior-connected to issue l versus r. For instance, since views on sports are not naturally connected with politics (i.e.,  $\mu_0(y|l) \approx \mu_0(y|r)$ ), views on which teams are most promising do not become more correlated with political leanings through social learning.<sup>19</sup> While there are potentially a range of beliefs within each community, for k sufficiently large and  $\mu_0(y|l) > \mu_0(y|r)$ , every member of the left-leaning community is more optimistic about y than all members of the right-leaning community.

To illustrate these results, consider the example from Section 3.1 where people interpret the data h = "a natural disaster struck and GDP growth this quarter was low." In our two-issue extension, sharing models that suggest the left-leaning candidate is better at governing leads members of the community to also interpret the data as suggesting that the economy is likely to grow next quarter. Conversely, sharing models that suggest the right-leaning candidate is better at governing leads members of the community to interpret the same data as suggesting that the economy is unlikely to grow. The right-leaning community's interpretation is that a natural disaster and low current growth are likely if the right-leaning candidate was better at governing (e.g., because the left-leaning party in power is incompetent). The left-leaning community's interpretation is that the data is likely if the left-leaning candidate is better at governing (e.g., because GDP growth could have been much worse in the face of a natural disaster). In other words, beliefs about the economy become "spurious implications" of beliefs about the candidate that governs better. Thus, shared belief communities lead to polarization and disagreement on issues beyond the issue driving community formation.

Consistent with this idea, there is sharp disagreement between Democrats and Republicans about economic conditions. For instance, Democrats report much higher consumer confidence before the 2016 election and after the 2020 election (when Democrats were president), while Republicans report much higher confidence between the two elections.<sup>20</sup>

<sup>&</sup>lt;sup>19</sup>For  $\mu_0(y|l) \approx \mu_0(y|r), \mu_0(l, y) = a \approx b = \mu_0(r, y)$ , so the simple average between the lowest and highest potential values of  $\mu_i^{\text{left-leaning}}(y) - \mu_j^{\text{right-leaning}}(y)$  across people *i* (in the left-leaning community) and *j* (in the right-leaning community) is given by the second line of Equation (1), given the assumption that  $k \geq \mu_0(l)/(\mu_0(l) + \mu_0(l, y))$ .

<sup>&</sup>lt;sup>20</sup>See Bartels (2002) and Gerber and Huber (2009) for systematic evidence. Evidence is mixed on whether

This pattern emerges in our framework if people discuss economic data within communities primarily formed based on partian affiliation.

These results may shed light on the so-called "polarization of reality" documented by Alesina et al. (2020). They show how the political left and right differ in their perceptions of, for example, the probability of upward social mobility. Our model suggests that such polarization is likely to occur along issues that the electorate believes are connected to whether the left or right governs better, as is naturally the case with social mobility since it connects to policy. Insofar as social media facilitates the formation of communities based on shared beliefs (increasing k), our model also suggests that it may play a role in increasing the polarization is *less* likely to occur with issues that the electorate believes are *not* connected to whether the left or right is likely to govern better (e.g., sports).

## 5 Managing Communication

We now turn to the implications of our framework for how someone could try to manage communication to her advantage. We call this person a "communications manager."

### 5.1 Managing Communication Through Messaging

We first consider managing communication through messaging. The key result is that messaging is most effective before social learning since it may impact the community a person joins. In other words, our framework provides a reason to "get in front of the news" by providing a favored interpretation.

To see this, consider shared-belief communities. Imagine that before joining such a community, person *i* with belief  $\mu'_i$  is weakly exposed to belief  $\tilde{\mu} \notin s(\mu'_i)$  with supporting model  $m(\tilde{\mu})$ . Following exposure to model  $m(\tilde{\mu})$ , the person potentially updates her beliefs and joins the shared-belief community associated with her posterior.

**Proposition 4.** Suppose everyone is maximally open to persuasion,  $M = M^a$ , and is in a shared-belief community. Let  $\mu_i$  denote a person's belief following social learning without being exposed to a belief  $\tilde{\mu} \notin s(\mu'_i)$ ,  $\mu^e_i$  denote her belief following social learning

these beliefs impact real outcomes, with Mian et al. (2023) finding no effect on consumption but Meeuwis et al. (2022) finding effects on investment portfolios.

after being exposed to belief  $\tilde{\mu}$ , and  $\mu_i^p$  denote her belief following social learning when exposed to belief  $\tilde{\mu}$  before social learning. If a person is persuaded through (weak or strong) exposure to  $\tilde{\mu}$  after social learning,  $\mu_i^e \neq \mu_i$ , then she is also persuaded through exposure to  $\tilde{\mu}$  before social learning,  $\mu_i^p \neq \mu_i$ . However, the converse does not hold.

This result says that exposing people to messaging (i.e., models supporting an alternative belief) is more likely to impact which shared-belief community they join and hence their final beliefs if exposure comes before they exchange models with others. To illustrate, return to the public-policy example (Ex. 2) with k = .75 as in Figure 1. If a person with an initial reaction  $\mu'_i(l) = .3$  is strongly exposed to belief  $\tilde{\mu} = .75$  before social learning, then she could join the left-leaning community and hold belief  $\mu_i^p = .75$  after social learning. However, if that same person was instead strongly exposed to belief  $\tilde{\mu} = .75$  after social learning, she would first join the center community, hold belief  $\mu_i = .5$ , and be unpersuadable,  $\mu_i^e = .5$ . The reason is simple: social learning hardens reactions to data, which inoculates people against finding models supporting alternative beliefs compelling. This may shed light on organizations' attempts to preemptively frame surprising news to avoid "losing control of the narrative." For example, firms often announce that a CEO unexpectedly resigned to "spend time with family." Firms also often have "culture training" for new employees before they socialize with existing employees. In our framework, these actions serve to provide early interpretations that imply favorable beliefs—e.g., the CEO's resignation does not imply the firm is in trouble-which in turn prevents people from hardening views within communities centered around less favorable beliefs. After social learning, people are less persuadable because their beliefs are supported by a better-fitting models. In other words, social learning makes people more certain that their interpretations of the data are correct and hence less open to other interpretations. A person who only talks to others who share the reaction that the latest school shooting indicates the need for stricter gun-control measures will become more confident in the rationale for drawing this conclusion from the data; a person who only talks to others who share the reaction that the shooting indicates the need for looser gun-control measures will similarly become more confident in drawing this conclusion from the data.<sup>21</sup>

<sup>&</sup>lt;sup>21</sup>In a sense, this is consistent with Schkade et al. (2007), which found that after group interactions views on climate change, affirmative action, and civil unions became more homogeneous and more confident. Some studies on such "group polarization" find that beliefs also become "more extreme" after group interactions. Proposition 2 is consistent with those findings insofar as extremity is measured by confidence and inconsistent

#### 5.2 Managing Communication by Influencing Communities

We next consider how a communications manager might directly influence the community structure by, for instance, inviting specific groups to meetings or preventing certain groups from forming. For example, a CEO might insist on being in all meetings with certain sub-ordinates. A key point is that the communications manager often faces a tradeoff between inducing people to take a specific action and inducing people to agree on the same model.

#### 5.2.1 Promoting Specific Actions

Suppose first that the communications manager wants to encourage people to take some action in response to the data. For example, in response to a school shooting, the manager might want to encourage interpretations that either support tightening gun control, the status quo, or loosening gun control. Or, following unexpectedly low earnings, a CEO may want to encourage followers to interpret the data as supporting cutting costs, staying the course, or investing in growth.

Formally, consider the case where each person has a finite action space and the communications manager's objective is a strictly monotonically increasing function of the fraction of people who choose her ideal action  $a^s \in A$ . How would the communications manager want to structure the community—i.e., the set of models  $M_i$  a given person i is exposed to—to maximize this objective?

**Proposition 5.** Suppose each person has a finite action space and the communications manager's objective is a strictly monotonically increasing function of the fraction of people who choose her ideal action  $a^s \in A$ . The communications manager cannot do better than, for every person *i*, exposing her to all people who would choose  $a^s$  in the absence of social learning, and exposing her to nobody else: That is, the communications manager's objective is maximized by setting

$$M_i = \{ m \in \bar{M}(h, \mu_0, d, M) : a(\mu(h, m)) = a^s \}$$
(2)

for all i. The communications manager's objective continues to be maximized by adding to

with those findings insofar as extremity is measured by how strongly beliefs react to data (if groups are formed based on shared beliefs and people have common priors). On this last point, Roux and Sobel (2015) shows how group polarization naturally arises in models of rational information aggregation.

 $M_i$  specified in Eq. (2) any model m with  $\Pr(h|m, \mu_0) < \max_{\tilde{m} \in M_i} \Pr(h|\tilde{m}, \mu_0)$ , but it is no longer maximized by adding a model m with  $\Pr(h|m, \mu_0) > \max_{\tilde{m} \in M_i} \Pr(h|\tilde{m}, \mu_0)$ .

This result says that the communications manager wants to expose people to all models that support taking action  $a^s$  and no other models. In particular, the communications manager does not want people to hear good-fitting arguments supporting other actions. For example, a firm CEO may want to control interpretations of earnings announcements by disproportionately calling on bullish analysts in earnings calls (Cohen et al. (2020)).

To illustrate these results, take the public-policy example (Ex. 2) above with  $\mu_0(l) = 1/2$  and a history h that under the default is perfectly diagnostic of the underlying state being l. Suppose the communications manager wants people to choose a = L. She should take individuals who would choose a = R in the absence of communication and surround them with people who would choose a = L in the absence of communication. For example, she should form communities where all people whose initial reactions are left-leaning  $(\mu(l) \ge .75)$  talk to each person whose initial reaction is right-leaning  $(\mu(r) > .75)$ . In this case, the right-leaning people would end up believing  $\mu(l) = .75$ . A key implication of our framework concerns whom the communications manager most wants to silence: people who support the status quo—i.e., those with  $\mu(l) \in (.25, .75)$ . These people will have arguments that fit the data given priors very well and support inaction.<sup>22</sup>

#### 5.2.2 Promoting Shared Models

By this logic, expanding people's communities could reduce polarization but also mute reactions to data that are open to interpretation. In the limit where a person is exposed to all possible models, the person will adopt a model that completely neutralizes the data: when data is open-to-interpretation and relevant for updating beliefs about  $\omega$  under the true model, expanding a person's shared-belief community further untethers her beliefs from reality. These results speak to the effects of increased connectedness between people

<sup>&</sup>lt;sup>22</sup>For example, suppose a school shooting could lead to a loosening or tightening of gun-control restrictions and the communications manager supports tighter gun control. The communications manager wants people arguing for tighter gun control to speak and everyone else to listen. The people the communications manager most wants to silence are moderates who argue for inaction, whether or not they are left- or right-leaning. Continuing this logic in a trivial dynamic extension, once all the people arguing for tighter gun control have spoken enough to harden beliefs, the communications manager is not worried about them having bilateral conversations with people favoring looser gun control—but they would still be wary of them having bilateral conversations with those who support the status quo.

generated by social media.

An implication is that promoting specific actions typically conflicts with promoting shared models. Because the status quo is favored by interpretations that fit the data perfectly and hence imply beliefs do not need to update, it can be hard to move people whose initial reaction is that the data supports the status quo. In contrast, if the communications manager simply wants people to end up with the same model—for instance, because she benefits when their actions are coordinated—then she should encourage open communication.

**Proposition 6.** Suppose the communications manager's objective is a strictly monotonicallyincreasing function of the fraction of people who share what ends up to be the most popular model. The communications manager cannot do better than, for every person *i*, exposing her to all models: That is, the communications manager's objective is maximized by setting for all *i* 

$$M_i = \overline{M}(h, \mu_0, d, M). \tag{3}$$

If the goal is for everyone to end up sharing the same model, the communications manager wants everyone to talk to each other and share their models. When receivers are maximally open to persuasion, this means that everyone will end up with interpretations that neutralize the data and promote the status quo. Note that this last point does not rely on the assumption that people hold common priors: When people are maximally open to persuasion with non-common priors, then it is still the case that the "h was inevitable" model is the only one that fits better than every other model represented in the population. And when everyone adopts this model, they stick with their prior beliefs and take the same action they would have taken in the absence of seeing the data h—i.e., they stick with their status-quo actions.

## 6 Applications

#### 6.1 When and How to Hold a Meeting

Why do organizations hold so many meetings? Economic models typically assume meetings are fundamentally about information exchange: One worker holds a piece of information that another does not and exchanging information helps workers adapt to the environment and coordinate their actions (e.g., Dessein and Santos (2006)). Under this view, meetings are essentially no different from other communication technologies (e.g., emails) and are called when workers do not share the same information set. After meetings, workers all agree on the optimal action, which is better adapted to the full information set.

Organizational scholars view meetings much more broadly. They come in different forms, such as town halls or all hands. They are sometimes about information exchange, but they are also about diagnosing problems, communicating organizational priorities, and exchanging or amplifying views on the right course of action.

Appendix E formalizes such a role for meetings, building on the view put forward in Weick (1995) that sensemaking is a fundamental activity of organizations. Following the logic of Section 5 costly meetings are called to help workers make sense of shared information. Meetings allow leaders to control interpretations workers share with each other, and they are called even when workers do not have any new private information. The key result that emerges is that the structure of meetings is not fixed but depends on workers' flow of communication outside meetings and how the organization prioritizes adapting to the environment versus coordinating among workers. In particular, leaders can find it optimal to use meetings to coordinate workers by muting their reactions to data, even if the leaders themselves interpret the data as suggesting the organization needs to better adapt to the environment.

#### 6.2 The Evolution and Spread of Misconceptions

Why do people believe in misconceptions (e.g., GMOs and vaccines are dangerous) and conspiracy theories (e.g., QAnon) when the Internet and social media also give them access to high-quality information? Echo chambers are a common answer to this question. While people have access to high-quality information, their media diets and social networks only expose them to misinformation and falsehoods. Under this view, falsehoods spread like viruses and crowd out the truth. People hear the same falsehood repeatedly and perhaps then overweight it.

An emerging literature suggests that this echo-chamber view is incomplete. Guess et al. (2018) argue that most Americans have diverse media diets, and that social media like Twitter tend to increase the diversity of viewpoints that people are exposed to. Similarly, Bertrand and Kamenica (2020) find that while social attitudes have become stronger predictors of political ideology over time, they have not become stronger predictors of media

diet. In addition, Boxell et al. (2017, 2020) find that while political polarization is increasing, it is not increasing faster for people who extensively use the Internet and social media. Thus, while echo chambers could be a concern, they may not be as widespread a problem as conventional wisdom portrays. The persistence of disagreement remains a puzzle not fully explained by echo chambers.

Our framework offers a different explanation, highlighting the difference between interpretations and information. Within a community, people are exposed to crowdsourced models that evolve to fit the data better and better, which makes them more certain their interpretation of the data is correct. Insofar as social media and the Internet make it easier to form shared-belief communities, our framework predicts that their primary impact will be to make people's beliefs resistant to change.

**Proposition 7.** Suppose person *i* and *j* hold the same beliefs  $\mu$ . If person *i* formed those beliefs through social learning in a shared-belief community and *j* formed those beliefs in some other way, then person *j* is (weakly) more persuadable than person *i*.

Proposition 7 says that shared-belief communities inoculate people against finding alternative beliefs compelling. The reason flows from a basic property of such communities: for every belief initially held by someone in the community, the best-fitting model supporting that belief (among models in M) is represented in the community. Combined with the earlier result that communities formed based on shared beliefs mute reactions (Proposition 2), this implies that shared-belief communities cause beliefs to be persistently untethered from data that is open to interpretation, creating a form of groupthink (Janis (2008)) whereby "all agents take the wrong action" (Harel et al. (2021)).<sup>23</sup> To make an analogy to viruses, communities lead interpretations to "mutate" to achieve better fit within the community—and people are exposed to more "variants" within than across communities.<sup>24</sup>

<sup>&</sup>lt;sup>23</sup>Other recent economic models of groupthink include Bénabou (2013), which views groupthink as arising from motivated mis-reading or neglect of evidence, and Harel et al. (2021), which views groupthink as arising from social learning of information from actions rather than from the exchange of private signals. In contrast to those models, we shed light on situations where shared beliefs and actions may be overly pessimistic (e.g., about the economy or political issues) and differ across communities that share similar facts (see, e.g., Angelucci and Prat (2024)).

<sup>&</sup>lt;sup>24</sup>Bowen et al. (2021) provide an alternative model where belief polarization is driven by misperceptions about selective sharing of second-hand information within an echo chamber. In Bowen et al. (2021), disagreement and polarization are driven by different people holding different information (having heterogeneous "information diets" of second-hand information) and not properly accounting for that fact; in our model, disagreement arises even when people share the same information. Their framework sheds light on situations

While we could illustrate these results by applying the baseline model we presented above, it is more revealing to consider a simple two-period dynamic extension of the analysis under the assumption that everyone is maximally open to persuasion. The key idea is that if communities form endogenously in response to one set of information, those communities will tend to encourage different interpretations of all future information. In other words, community formation based on shared-prior beliefs creates strong path dependence in the way people interpret information.

Formally, suppose people begin with the same priors, react to data  $h_1$ , and form shared belief communities based on their reactions to  $h_1$ . Further suppose that after exchanging models through the community, people's posterior beliefs after interpreting  $h_1$  become their priors in interpreting new data  $h_2$ . In interpreting  $h_2$ , people share models with others in the shared-belief community that was formed based on common reactions to earlier data  $h_1$ . That is, communities are sticky across the two periods: people stay in the sharedbelief community that was formed in period 1. For example, people may talk to others who share a similar reaction to evidence purporting to show a relationship between vaccines and autism and continue to talk to the same people when new data arrives.

The key result from this dynamic extension is that communities have lasting consequences on how people interpret subsequent events. By Proposition 2, everyone within a given shared-belief community ends up holding the initial belief closest to the prior within that community in response to data  $h_1$ . So everyone within a shared-belief community begins with the same prior entering into the second period where they interpret data  $h_2$ . Call this prior belief  $\mu_1^s$ , which differs across communities s. Since people use the same community to exchange interpretations of  $h_2$ , social learning maximally mutes and hardens a person's reaction to the data. In other words, everyone ends up at the belief they held prior to seeing  $h_2$  with a model that perfectly explains the data: for every person i in shared belief community s,  $\mu_i = \mu_1^s$  and  $\Pr(h_2|m_i, \mu_1^s) = 1$ .

This analysis suggests that once misconceptions evolve and harden within a community through crowdsourced interpretations of a high-profile event, members of that community explain subsequent events in a way that makes them consistent with the original interpretation. In other words, a bad take on an event can be very hard to reverse: Once a person

where a lot of news is coming out each day and it is hard to keep track of it all (e.g., if there is a war or people are forming beliefs about a new political candidate). We shed light on situations where the basic facts are essentially common knowledge and people are primarily exchanging interpretations of those facts.

"goes down the rabbit hole", it is difficult to use new information or interpretations to convince them to come out. Indeed, recent papers (Nyhan et al. (2023); Guess et al. (2023)) find that temporarily (e.g., around elections) reducing people's exposure to like-minded content and increasing their exposure to counterattitudinal content does not appreciably impact their beliefs. In our framework, this resistance to change emerges because before the intervention the community already exposed people to interpretations that fit their prior knowledge well.

### 7 Discussion

This paper is a first step to studying the social transmission of models. There are several potential avenues for future work. For instance, while we assume people costlessly exchange models, people often devote time and effort seeking new models for reasons of curiosity, identity, and instrumentality. How does a realistic demand function for models influence, for example, the way communities are structured?

We also show prior beliefs shape initial reactions to the data, community formation, and ultimately reactions after social learning. But, other than in our dynamic extension in Section 6.2, we say little about where these priors come from. What we do shed light on is why beliefs often appear stable in the face of contradictory, but open-to-interpretation, data. And we make the novel (to our knowledge) prediction that initial beliefs will respond to such data before reverting towards the prior.

To isolate the impact of social learning of models, we assume that all information is public. In some contexts, social learning involves sharing both models and private information. Social learning in such contexts has two effects: It makes private information public, as in most of the literature, and it frames information, as in our model. The scope for social learning to lead to more accurate beliefs increases in the degree to which there is private information that is closed to interpretation.

We focus on shared-belief communities because they capture important features of realworld groups. But some communities are instead formed based on shared models. Some communities of venture capitalists primarily evaluate startups based on product attributes, while others focus on attributes of founders. How do communities shape views in such cases? Appendix B.3 analyzes a special class of shared models, in which people are dogmatic on how to interpret certain types of information. The key result is that people end up reacting only to the data that they are inflexible in interpreting. Quantitative analysts will talk to other quantitative analysts about how to interpret qualitative information and end up agreeing that, while it initially seemed relevant, it is not useful.

The framework also admits further applications. For example, how should a manager organize teams to arrive at a realistic interpretation of the data? A loose intuition reminiscent of Hong and Page (2001) that arises from our framework is that aggregating across teams that have different ways of looking at the data (i.e., different models) may be more helpful than aggregating across teams that are systematically trying to come to different *conclusions* from the data. For instance, in the venture capital context, it may be helpful to have people who focus on management team experience and people who focus on current profits. It is unlikely to be helpful to have people who always want to invest and people who never want to invest, each of whom comes up with the interpretation of the data that best supports their (pre-specified) conclusion.

### A Proofs

Proof of Proposition 1. When  $\tilde{h}$  is realized, any model in M must satisfy  $\Pr(\tilde{h}_k | \tilde{h}_1, m', \mu_0) \le 1$  (logic of probability) and  $\Pr(\tilde{h}_k | m', \mu_0) = \pi_k(\tilde{h}_k)$  (definition of M). This means that

$$\max_{m \in M} \Pr(\tilde{h}_k | \tilde{h}_1, m, \mu_0) - \Pr(\tilde{h}_k | m, \mu_0) \le 1 - \pi_k(\tilde{h}_k) \ \forall \ k.$$
(4)

If a model  $m' \in M$  achieves the right side of (4), then any best-fitting model in M must also achieve it:  $\Pr(\tilde{h}|m,\mu_0) \leq \pi_1(\tilde{h}_1) = \Pr(\tilde{h}|m',\mu_0)$ . Under any such model m' that additionally has the property that  $\pi_{m'}(\tilde{h}_1|\omega)$  is constant across values of  $\omega$ , people's posterior beliefs equal their prior beliefs  $\mu_0$  because likelihoods would then be independent of  $\omega$ .

It remains to show that there is in fact a model  $m' \in M$  that (i) achieves the right side of (4) and (ii) has the property that  $\pi_{m'}(\tilde{h}_1|\omega)$  is constant across values of  $\omega$ . Letting  $h_{-1} \equiv (h_2, \ldots, h_N)$ , it is easy to check that the following is such a model:

$$\pi_{m'}(\tilde{h}|\omega) = \pi_{1}(\tilde{h}_{1}) \ \forall \omega$$
  

$$\pi_{m'}(\tilde{h}_{1}, h_{-1}|\omega) = 0 \ \forall \ h_{-1} \neq \tilde{h}_{-1}, \ \omega$$
  

$$\pi_{m'}(h_{1}, \tilde{h}_{-1}|\omega) = \frac{\pi_{1}(h_{1})}{1 - \pi_{1}(\tilde{h}_{1})} \times \left[ \Pr(\tilde{h}_{-1}|m^{T}, \mu_{0}) - \pi_{1}(\tilde{h}_{1}) \right] \ \forall \ h_{1} \neq \tilde{h}_{1}, \ \omega$$
  

$$\pi_{m'}(h_{1}, h_{-1}|\omega) = \frac{\pi_{1}(h_{1})}{1 - \pi_{1}(\tilde{h}_{1})} \times \left[ \Pr(h_{-1}|m^{T}, \mu_{0}) \right] \ \forall h_{1} \neq \tilde{h}_{1}, \ h_{-1} \neq \tilde{h}_{-1}, \ \omega.$$

*Proof of Proposition 2.* Consider an arbitrary person *i* and let

MovementMin<sub>i</sub> 
$$\equiv \arg \min_{\mu \in s(\mu'_i)} Movement(\mu; \mu_0).$$

Someone in *i*'s network will propose a model  $\tilde{m}$  that maximizes  $\Pr(h|\cdot, \mu_0)$  subject to  $\mu(h, \tilde{m}) \in \text{MovementMin}_i$ . By Lemma 1, this model will fit strictly better than all models represented in *i*'s network that imply beliefs outside of MovementMin<sub>i</sub>, so everyone in *i*'s network will adopt models that imply beliefs in MovementMin<sub>i</sub>.

*Proof of Proposition 3.* 1. For every  $\tilde{\mu}$ , there exists a positive measure of models  $m(\tilde{\mu})$  supporting that belief that are less compelling than the model  $m_i$  a person would adopt prior to weak exposure to that belief: for example, take models

$$\pi_{m(\tilde{\mu})}(h|\omega) = \frac{\tilde{\mu}(\omega)}{\mu_0(\omega)} \cdot (\Pr(h|m_i, \mu_0) - \varepsilon)$$

for all  $\omega \in \Omega$  and for  $\varepsilon > 0$  small.

2. When  $\tilde{\mu}$  is closer to the person's prior, as measured by Movement $(\cdot; \mu_0)$ , than any belief supported by a model in  $M_i$ , then the best-fitting model supporting  $\tilde{\mu}$  fits better than any model in  $M_i$  (by Lemma 1).

Proof of Corollary 1. Let

$\mu^{\text{left-leaning}}$	$\mid n$	y
l	$a^L$	$b^L$
r	$c^L$	$d^L$

denote a movement-minimizing belief of members of the left-leaning network and

$\mu^{\text{right-leaning}}$	n	y
l	$a^R$	$b^R$
r	$c^R$	$d^R$

denote a movement-minimizing belief among members of the right-leaning network.

For the left-leaning network,  $\mu^{\text{left-leaning}}(l) = a^L + b^L \ge k$ . Assuming, as we will later establish, that Movement( $\mu^{\text{left-leaning}}; \mu_0$ ) = max  $\{a^L/a, b^L/b\}$ , then the inequality must bind, so  $b^L = k - a^L$ . This then implies that Movement( $\mu^{\text{left-leaning}}; \mu_0$ ) = max  $\{a^L/a, (k - a^L)/b\}$ , which will be minimized when  $a^L/a = (k - a^L)/b \Rightarrow a^L = k \times a/(a + b) = k \times \mu_0(n|l)$  and  $b^L = k \times b/(a + b) = k \times \mu_0(y|l)$ .

Summarizing what we know so far:

$\mu^{\text{left-leaning}}$	n	y	$\mu^{\text{left-leaning}}$	n	y
l	$k \times \frac{a}{a+b}$	$k \times \frac{b}{a+b}$	= l	$k \times \mu_0(n l)$	$k \times \mu_0(y l)$
r	$c^L$	$d^L$	r	$c^L$	$d^L$

and we can similarly establish that

$\mu^{\text{right-leaning}}$	n	y	$\mu^{\text{right-leaning}}$	n	y
l	$a^R$	$b^R$	= l	$a^R$	$b^R$
r	$k \times \frac{c}{c+d}$	$k \times \frac{d}{c+d}$	r	$k \times \mu_0(n r)$	$k \times \mu_0(y r)$

Proceeding further,  $c^L$  and  $d^L$  must satisfy the following constraints if the premise above is true that Movement $(\mu^{\text{left-leaning}}; \mu_0) = \max \{a^L/a, b^L/b\}$ :

$$c^{L} + d^{L} = (1 - k) \Rightarrow d^{L} = (1 - k) - c^{L}, \text{ and}$$
$$\max\left\{c^{L}/c, d^{L}/d\right\} = \max\left\{\frac{c^{L}}{c}, \frac{(1 - k) - c^{L}}{d}\right\} \le \max\left\{a^{L}/a, (k - a^{L})/b\right\} = \frac{k}{\mu_{0}(l)},$$

where the last equality follows from plugging in  $a^L$  from the earlier calculations and, here,  $c = \mu_0(r, n), d = \mu_0(r, y)$ . The range of  $c^L$  that satisfy these conditions is given by

$$\max\left\{0, (1-k) - k \times \frac{\mu_0(r, y)}{\mu_0(l)}\right\} \le c^L \le \min\left\{1 - k, k \times \frac{\mu_0(r, n)}{\mu_0(l)}\right\},\$$

which is non-empty given the assumptions that  $k \ge \mu_0(l) = 1/2$ . This last fact also establishes the premise that  $Movement(\mu^{left-leaning}; \mu_0) = \max \{a^L/a, b^L/b\}$ .

We can similarly derive that

$$\max\left\{0, (1-k) - k \times \frac{\mu_0(r, n)}{\mu_0(l)}\right\} \le d^L \le \min\left\{1 - k, k \times \frac{\mu_0(r, y)}{\mu_0(l)}\right\} \\ \max\left\{0, (1-k) - k \times \frac{\mu_0(l, y)}{\mu_0(r)}\right\} \le a^R \le \min\left\{1 - k, k \times \frac{\mu_0(l, n)}{\mu_0(r)}\right\} \\ \max\left\{0, (1-k) - k \times \frac{\mu_0(l, n)}{\mu_0(r)}\right\} \le b^R \le \min\left\{1 - k, k \times \frac{\mu_0(l, y)}{\mu_0(r)}\right\}.$$

Taken together,

$$\begin{split} \mu^{\text{left-leaning}}(y) &\geq \max\left\{k \times \mu_0(y|l), k \times \mu_0(y|l) + (1-k) - k \times \frac{\mu_0(r,n)}{\mu_0(l)}\right\}\\ \mu^{\text{left-leaning}}(y) &\leq \min\left\{k \times \mu_0(y|l) + 1 - k, k \times \mu_0(y|l) + k \times \frac{\mu_0(r,y)}{\mu_0(l)}\right\}\\ \mu^{\text{center-leaning}}(y) &= \mu_0(y)\\ \mu^{\text{right-leaning}}(y) &\geq \max\left\{k \times \mu_0(y|r), k \times \mu_0(y|r) + (1-k) - k \times \frac{\mu_0(l,n)}{\mu_0(r)}\right\}\\ \mu^{\text{right-leaning}}(y) &\leq \min\left\{k \times \mu_0(y|r) + 1 - k, k \times \mu_0(y|r) + k \times \frac{\mu_0(l,y)}{\mu_0(r)}\right\}. \end{split}$$

This then means that

$$\begin{split} \mu^{\text{left-leaning}}(y) &- \mu^{\text{right-leaning}}(y) \ge \max\left\{k \times \mu_0(y|l), k \times \mu_0(y|l) + (1-k) - k \times \frac{\mu_0(r,n)}{\mu_0(l)}\right\} \\ &- \min\left\{k \times \mu_0(y|r) + 1 - k, k \times \mu_0(y|r) + k \times \frac{\mu_0(l,y)}{\mu_0(r)}\right\}. \end{split}$$

Assuming that  $\mu_0(l) = 1/2$  and  $\mu_0(l,y) = \mu_0(r,n) \Rightarrow \mu_0(y|l) = \mu_0(n|r)$ , then this inequality reduces to

$$\mu^{\text{left-leaning}}(y) - \mu^{\text{right-leaning}}(y) \ge \begin{cases} 2k \times \mu_0(y|l) - 1 & \text{if } k \ge \frac{\mu_0(r)}{\mu_0(r) + \mu_0(l,y)} \\ (1 - 2k) & \text{if } k < \frac{\mu_0(r)}{\mu_0(r) + \mu_0(l,y)}. \end{cases}$$

We also have

$$\mu^{\text{left-leaning}}(y) - \mu^{\text{right-leaning}}(y) \le \min\left\{k \times \mu_0(y|l) + 1 - k, k \times \mu_0(y|l) + k \times \frac{\mu_0(r, y)}{\mu_0(l)}\right\} - \max\left\{k \times \mu_0(y|r), k \times \mu_0(y|r) + (1 - k) - k \times \frac{\mu_0(l, n)}{\mu_0(r)}\right\}.$$

Assuming that  $\mu_0(l) = 1/2$  and  $\mu_0(l, y) = \mu_0(r, n) \Rightarrow \mu_0(y|l) = \mu_0(n|r)$ , then this inequality reduces to

$$\mu^{\text{left-leaning}}(y) - \mu^{\text{right-leaning}}(y) \le \begin{cases} 2k \times (\mu_0(y|l) - 1) + 1 & \text{if } k \ge \frac{\mu_0(l)}{\mu_0(l) + \mu_0(r,y)} \\ k \times (1 + \mu_0(y|l) + \mu_0(y|r)) - 1 & \text{if } k < \frac{\mu_0(l)}{\mu_0(l) + \mu_0(r,y)}. \end{cases}$$

If  $k \geq \frac{\mu_0(l)}{\mu_0(l) + \mu_0(r,y)}$ , then the middle point between the lower and upper bound of  $\mu^{\text{left-leaning}}(y) - \mu^{\text{right-leaning}}(y)$ equals

$$k \times (2 \times \mu_0(y|l) - 1) = k \times (\mu_0(y|l) - \mu_0(y|r)),$$

while for  $\frac{\mu_0(r)}{\mu_0(r)+\mu_0(l,y)} \le k \le \frac{\mu_0(l)}{\mu_0(l)+\mu_0(r,y)}$  this middle point equals

$$k \times (\mu_0(y|l) + 1) - 1 = \frac{1}{2} \times k \times (\mu_0(y|l) - \mu_0(y|r) + 3) - 1.$$

Moreover, for  $k \ge \frac{1}{2 \times \mu_0(y|l)} \ge \frac{\mu_0(l)}{\mu_0(l) + \mu_0(l,y)}$ , simple algebra reveals that the lower bound of  $\mu^{\text{left-leaning}}(y) - \mu^{\text{right-leaning}}(y)$  is greater than 0.

*Proof of Proposition 4.* Weak exposure to belief  $\tilde{\mu}$  prior to social learning impacts the person's final beliefs if and only if the person finds  $m(\tilde{\mu})$  more compelling than the model  $m'_i$  she currently has in mind supporting belief  $\mu'_i$ : that is, if and only if

$$\Pr(h|m(\tilde{\mu}),\mu_0) > \Pr(h|m'_i,\mu_0).$$
(5)

Weak exposure to belief  $\tilde{\mu}$  following social learning impacts the person's final beliefs if and only if the person finds  $m(\tilde{\mu})$  more compelling than the best-fitting model among those represented in shared-belief network  $s(\mu'_i)$ : that is, if and only if

$$\Pr(h|m(\tilde{\mu}),\mu_0) > \max_{m' \in \bigcup_{\mu \in s(\mu'_i)} M(\mu)} \Pr(h|m',\mu_0).$$
(6)

The result follows from the right-hand-side of inequality (6) being larger than the right-hand-side of inequality (5).

A similar proof applies to the case of strong exposure to beliefs, replacing the left-handsides of inequalities (5) and (6) with  $\max_{m' \in M(\tilde{\mu})} \Pr(h|m', \mu_0)$ .

*Proof of Proposition 5.* The communication manager's objective is clearly maximized by exposing everybody to the best-fitting model that supports action  $a^s$  and exposing them to no other models. The communication manager does no worse by exposing people to all models specified in Eq. (2) (i.e., all models that support action  $a^s$ ), since this includes the best-fitting one and no models that support other actions. That is, everybody's behavior is

the same whether they are only exposed to the best-fitting model that supports  $a^s$  or models specified in Eq. (2). This remains true if we add to models specified in (2) any model mwith  $\Pr(h|m, \mu_0) < \max_{\tilde{m} \in M_i} \Pr(h|\tilde{m}, \mu_0)$ , since nobody will adopt such a model. However, the communication manager's payoff is strictly worse if we add to models specified in (2) any model m with  $\Pr(h|m, \mu_0) > \max_{\tilde{m} \in M_i} \Pr(h|\tilde{m}, \mu_0)$ , since anybody who would've adopted a model in  $M_i$  will instead adopt this model which supports taking an action other than  $a^s$ .

*Proof of Proposition 6.* If everybody is exposed to  $\overline{M}(h, \mu_0, d, M)$ , then everybody will also end up adopting the model in that set that maximizes  $\Pr(h|\cdot, \mu_0)$ . The communication manager cannot do better, since everyone will end up sharing the same model.

*Proof of Proposition 7.* If person *i* forms her beliefs  $\mu$  in a shared-belief network, then she adopts the best fitting model in *M* that supports those beliefs. The fit of person *j*'s model supporting those beliefs must then fit weakly less well than person *i*'s, which makes her weakly more persuadable.

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# Sharing Models to Interpret Data: Online Appendices

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# **B** Model Details

#### **B.1 Initial Reactions**

Let  $\bar{\Delta}(h, \mu_0, d, M) = \{\mu \in \Delta(\Omega) : \mu = \mu(h, m) \text{ for some } m \in \bar{M}(h, \mu_0, d, M)\}$  denote the set of initial beliefs in reaction to the data. By assumption, fraction  $\delta$  of the population sticks with the default and holds beliefs  $\mu(h, d)$  and fraction  $(1 - \delta)$  holds beliefs in  $\bar{\Delta}(h, \mu_0, d, M)$ .

Proposition A.1. The set of initial beliefs in reaction to the data is a subset of

$$\bar{\bar{\Delta}}(h,\mu_0,d,M) = \left\{ \mu \in \Delta(\Omega) : \mu(\omega) \le \frac{\mu_0(\omega)}{\Pr(h|d,\mu_0)} \,\forall\, \omega \in \Omega \right\}.$$

Further, when people are maximally open to persuasion given the data,  $M = M^a$ , we have  $\bar{\Delta}(h, \mu_0, d, M) = \bar{\Delta}(h, \mu_0, d, M)$ .

*Proof of Proposition A.1.* This proof is essentially the same as the proof of Proposition 1 in Schwartzstein and Sunderam (2021). We repeat it here for completeness.

Note that

$$\mu(\omega|h,m) = \frac{\pi_m(h|\omega) \cdot \mu_0(\omega)}{\Pr(h|m,\mu_0)}$$

by Bayes' Rule. Since  $\pi_m(h|\omega) \leq 1$  and, by definition of  $\overline{M}(h, \mu_0, d, M)$ ,  $\Pr(h|m, \mu_0) \geq \Pr(h|d, \mu_0)$  for all  $m \in \overline{M}(h, \mu_0, d, M)$ , beliefs that do not lie in  $\overline{\Delta}(h, \mu_0, d, M)$  cannot be included in  $\overline{\Delta}(h, \mu_0, d, M)$ . To see that for rich enough M, all beliefs in  $\overline{\Delta}(h, \mu_0, d, M)$  are also in  $\overline{\Delta}(h, \mu_0, d, M)$ , define m by

$$\pi_m(h|\omega) = \frac{\mu(\omega|h,m)}{\mu_0(\omega)} \times \Pr(h|d,\mu_0) \; \forall \omega \in \Omega.$$

Proposition A.1, which is essentially a restatement of Proposition 1 in Schwartzstein and Sunderam (2021), characterizes the set of initial reactions to the data.<sup>1</sup>

#### **B.2** Expanding Communities

Expanding person *i*'s community by merging it with  $\tilde{M}$  enlarges the set of models that are shared with person *i* to  $M_i \cup \tilde{M}$ .

**Proposition A.2.** Suppose everyone is maximally open to persuasion,  $M = M^a$ . Let  $\mu_i$   $(m_i)$  denote a person's belief (model) following social learning prior to a community expansion, and  $\mu_i^e$   $(m_i^e)$  denote her belief (model) following social learning with the expanded community.

- 1. Expanding person i's community in any way weakly hardens her reaction to the data: for any expansion of  $M_i$  to  $M_i \cup \tilde{M}$  with  $\tilde{M} \subset M$ ,  $\Pr(h|m_i^e, \mu_0) \ge \Pr(h|m_i, \mu_0)$ .
- 2. If, in addition, everyone is in a shared-belief community, then expanding person *i*'s community in any way also weakly mutes her reaction to the data: for any expansion of  $M_i$  to  $M_i \cup \tilde{M}$  with  $\tilde{M} \subset M$ , Movement $(\mu_i^e; \mu_0) \leq Movement(\mu_i; \mu_0)$ .

Proof of Proposition A.2. 1. That expanding person *i*'s community hardens her reaction to data follows from the simple fact that  $\max_{m \in M^e} \Pr(h|m, \mu_0) \ge \max_{m \in M} \Pr(h|m, \mu_0)$ whenever  $M^e \supset M$ .

<sup>&</sup>lt;sup>1</sup>To derive the distribution over initial reactions, we need to additionally specify the distribution of models people initially come up with. Many of our results on beliefs after social learning are independent of this distribution.

2. That expanding person *i*'s community if anything mutes her reaction to the data when she's in a shared-belief community follows from the fact that  $m_i$  is the best-fitting model inducing  $\mu_i$ , which fits better than any model inducing a belief further from her prior according to Movement( $\cdot; \mu_0$ ) (by Lemma 1).

The first part of Proposition A.2 shows that expanding a community always (weakly) hardens a community member's beliefs and makes them less persuadable. The most basic impact of increasing connectedness in our model is increasing a person's view that she can explain the data and making her resistant to changing her mind. The second part of the proposition shows that when communities are based on shared beliefs, expanding the community always additionally mutes members' beliefs. Being exposed to more models increases fit and consequently reduces movement.

#### **B.3** Shared Model Communities

Some communities are based not on shared beliefs, but shared models. To analyze sharedmodel communities, consider a partition C over the set of admissible models M, where we denote c(m) as the element in  $\mathcal{M}$  that model  $m \in M$  belongs in. In a *shared-model* community, a person *i* exchanges models with another person *j* if and only if their initial models are similar, in the sense that they fall in the same element of  $\mathcal{M}$ .

**Definition A.1.** In a *shared-model community*,  $M_i = \{m \in \overline{M}(h, \mu_0, d, M) : m \in c(m'_i)\}$  for every person *i*.

People in a given shared model community will end up agreeing on whichever model in c(m) maximizes  $\Pr(h|\cdot, \mu_0)$ .

Decompose h into two types of data,  $h^a$  and  $h^b$ . In predicting the success of a project, stock, or politician, for example, there may be both quantitative or hard information, as well as qualitative or soft information. In interpreting whether a left- or right-leaning policy is better, there may be data communicated by left-leaning and right-leaning outlets.

Imagine there are communities that view  $h^a$  as open to interpretation, but not  $h^b$ , and vice-versa. Quantitative analysts may believe they have a good handle on how to interpret hard information but may be more open to different ways of thinking about qualitative information. Symmetrically, qualitative analysts may have a single interpretation of soft

interpretations but be open to many interpretations of hard information. People on the left may believe they know how to interpret left-leaning information, e.g., as trustworthy, but may be less sure on how to interpret right-leaning information. More formally, suppose there are three categories of models:

$$c^{A} = \left\{ m \in \bar{M}(h, \mu_{0}, d, M) : \pi_{m}(h^{a}, h^{b}|\omega) = \pi_{m}(h^{b}|\omega) \cdot \pi_{m^{fa}}(h^{a}|\omega) \forall \omega \in \Omega \right\}$$
  

$$c^{B} = \left\{ m \in \bar{M}(h, \mu_{0}, d, M) : \pi_{m}(h^{a}, h^{b}|\omega) = \pi_{m}(h^{a}|\omega) \cdot \pi_{m^{fb}}(h^{b}|\omega) \forall \omega \in \Omega \right\}$$
  

$$c^{O} = \bar{M}(h, \mu_{0}, d, M) \setminus \left\{ c^{A}, c^{B} \right\}.$$

The first category of models,  $c^A$ , has a fixed interpretation  $m^{fa}$  of  $h^a$  but differing interpretations of  $h^b$ . Conversely, category  $c^B$  has a fixed interpretation  $m^{fb}$  of  $h^b$  but differing interpretations of  $h^a$ . Finally, category  $c^O$  contains all other models. If shared inflexibility stems from shared expertise, it is natural to assume  $m^{fa} = m^T$  and  $m^{fb} = m^T$ ; if it stems from shared beliefs that the data is uninformative, it is natural to assume that  $m^{fa}$  renders  $h^a$  uninformative and  $m^{fb}$  renders  $h^b$  uninformative; if it stems from shared trust in knowing the process, it's natural to assume  $m^{fa} = d$  and  $m^{fb} = d$ .

Supposing the data is maximally open to persuasion,  $M = M^a$ , then people with initial models in  $c^A$  will end up convincing themselves that  $h^b$  is obvious in hindsight and hence uninformative, while people with initial models in  $c^B$  will end up analogously convincing themselves that  $h^a$  is uninformative.

**Proposition A.3.** Suppose everyone is maximally open to persuasion,  $M = M^a$ , and is in a shared-model community based on shared inflexibility of the form described above, where  $c(m) \in \{c^A, c^B, c^O\}$ . Then social learning need not moderate everyone's reaction to the data. In particular, social learning leads members of  $c^A$  to view  $h^b$  as uninformative, members of  $c^B$  to view  $h^a$  as uninformative, and members of  $c^O$  to view h as uninformative, resulting in final beliefs:

$$\mu_i = \begin{cases} \mu(h^a, m^{fa}) & \text{if } m'_i \in c^A \\ \mu(h^b, m^{fb}) & \text{if } m'_i \in c^B \\ \mu_0 & \text{if } m'_i \in c^O \end{cases}$$

Proof of Proposition A.3. Recall that

$$c^{A} = \left\{ m \in \bar{M}(h, \mu_{0}, d, M) : \pi_{m}(h^{a}, h^{b}|\omega) = \pi_{m}(h^{b}|\omega) \cdot \pi_{m^{fa}}(h^{a}|\omega) \; \forall \; \omega \in \Omega \right\}.$$

Clearly, the best fitting model in  $c^A$  is  $\pi_m(h^a, h^b|\omega) = 1 \cdot \pi_{m^{fa}}(h^a|\omega) = \pi_{m^{fa}}(h^a|\omega)$  for all  $\omega \in \Omega$ . Similarly, the best fitting model in  $c^B$  is  $\pi_m(h^a, h^b|\omega) = 1 \cdot \pi_{m^{fb}}(h^b|\omega) = \pi_{m^{fb}}(h^b|\omega)$  for all  $\omega \in \Omega$ . Finally, the best fitting model in  $c^O$  is  $\pi_m(h^a, h^b|\omega) = 1$  for all  $\omega \in \Omega$ . By assumption, someone in each community will propose the associated bestfitting models which all community members will end up adopting. The final beliefs  $\mu_i$ follow.

As an illustration, consider communities based on shared expertise and imagine a company will either be successful ( $\omega = 1$ ) or unsuccessful ( $\omega = 0$ ) with equal probability ex ante. People are trying to forecast the success of the company based on hard,  $h^a \in \{\underline{h}^a, \overline{h}^a\}$ , and soft,  $h^b \in \{\underline{h}^b, \overline{h}^b\}$ , information. The true probability of  $h^a$  being  $\overline{h}^a$  or  $h^b$  being  $\overline{h}^b$  is .75 conditional on future success and .25 conditional on future failure, where hard and soft signals are conditionally independent. Imagine that the hard and soft signals point in opposite directions, with the hard signal being truly good ( $h^a = \overline{h}^a$ ) and the soft signal being bad ( $h^b = \underline{h}^b$ ). Then, the correct response is to predict the probability of future success to be 1/2.

People's initial reactions to these signals will vary significantly. However, by Proposition A.3, the community of soft-information experts will settle on explaining away the hard information and come to believe the likelihood of future success to be 1/4. Conversely, the community of hard-information experts will settle on explaining away the soft information and come to believe the likelihood of future success to be 3/4. The non-experts will settle on explaining away all information and believing the likelihood of future success to be 1/2. Since some people in the hard- and soft-information communities will start with more moderate (and correct) reactions, in this example social learning intensifies some opinions in the hard- and soft-model communities in addition to hardening them.

With re-labeling, a similar example perhaps sheds light on so-called "epistemic closure" in political debates. Political observers argue that, in recent years, many of beliefs held by conservatives and liberals seem divorced from reality. Pundit Jonathan Chait puts it in the

following way:

the problem is that the [conservative] movement has created its own subculture, and within this subculture, only information from sources controlled by the movement is considered trustworthy or even worth paying attention to.<sup>2</sup>

The key problem, as Chait puts it, is *not* necessarily that liberals are unaware of information provided by conservatives and vice-versa, but rather that they hold shared beliefs that information from the other side of the aisle is not worth grappling with. The analysis in this section shows that this would be a consequence of shared inflexibility in believing information from your own side is trustworthy. Under this interpretation, liberals are aware of conservative information. And they begin with quite diverse opinions on how to interpret conservative information. But, in exchanging interpretations, they end up settling on a shared view that they should not update based on that information.

A final example of communities based on shared models is where the measure  $(1 - \delta)$  of the population who initially stick with the default are in one community and the rest of the population are in others. For example, some portion of the population may not devote enough attention to an issue to construct their own interpretation of the data beyond the default, nor to exchanging interpretations with others.

When the default is accurate (e.g., in some cases taking scientific consensus at face value), people who adhere to the default end up with more accurate interpretations and beliefs than those in other communities. For example, a 2016 Pew report found that Americans "who care a great deal about GM foods issue expected negative effects from these foods," belying scientific consensus. Similarly, Fernbach et al. (2019) found that people who are extremely opposed to GM foods think they know the most about the safety of those foods, but actually know the least. Such Americans pushed a number of unfounded interpretations of the data, including that eating GM foods caused allergies, cancer, and autism.

## C An Additional Example

This example shows how interpretations may evolve differently across shared-belief communities. Consider a community of venture capitalists trying to predict the success of a

<sup>&</sup>lt;sup>2</sup>https://newrepublic.com/article/74492/what-conservative-epistemic-closure-means

startup in a new sector (e.g., generative AI) based on the history of past startups and their characteristics. The characteristics of startup j are its profits  $(x_{1j})$ , management team experience  $(x_{2j})$ , and an individuating characteristic  $(x_{3j})$ —a characteristic that is unique to each startup. The history of past startups is  $h = \{(x_{1j}, x_{2j}, x_{3j}, y_j)\}_j$  where  $y_j = 1$  if startup j succeeded and  $y_j = 0$  if it failed. Figure A.1a shows an example history. Each dot represents a previous startup, with profit plotted on the horizontal axis and team experience plotted on the vertical axis. The individuating characteristics are not pictured. A dot is filled in if the startup was successful and is unfilled if it failed. Venture capitalists start with a prior that a given startup's probability of success,  $\theta$ , is uniformly distributed on [0, 1] and dogmatically believe that (profit) x (experience) characteristics are uniformly distributed in  $[0, 1] \times [0, 1]$ . They then use the history to make predictions about a new startup k's success probability as a function of its characteristics.

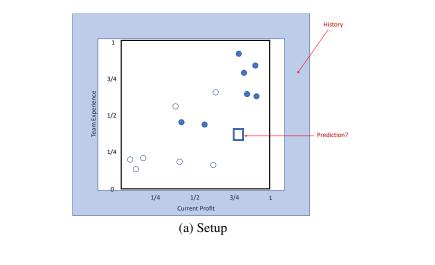
We assume there are four types of models in the model space M. First, the default model is that all startups in the new sector have the same success probability regardless of their characteristics. Second, there are models that are cutoff rules in profit: all startups with profit below the cutoff share the same success probability and all startups with profit above the cutoff share the same success probability.<sup>3</sup> For instance, the vertical green line in Figure A.1b depicts the model where the cutoff is the 25th percentile of profits. Third, there are models that are analogous cutoff rules in team experience. For instance, the horizontal red line in Figure A.1c depicts the model where the cutoff is the 25th percentile of experience. Fourth, there is a model positing that neither profits nor experience matter. Instead, each startup's outcome is due to its individuating characteristics; in other words, each startup had a unique feature that perfectly determined success or failure. Note that this model perfectly explains each data point.<sup>4</sup>

Prior to social learning, venture capitalists consider the default and one other model randomly selected from the other three model types. As shown in Figure A.1d, venture capitalists will have a variety of different interpretations, and thus different beliefs, at this point. In the figure, we depict for simplicity the case where the cutoffs considered are at the 25th, 50th, and 75th percentiles of each dimension. All fit better than the default.

Suppose venture capitalists are in shared-belief communities. Specifically, they share

<sup>&</sup>lt;sup>3</sup>Formally, success probabilities below and above the cutoff are independently drawn from the uniform distribution.

<sup>&</sup>lt;sup>4</sup>Formally, under the model  $m^{ind}$ ,  $\Pr(y|x_3, m^{ind}, \mu_0) = 1$  for  $y \equiv (y_j)_j$  and  $x_3 \equiv (x_{3j})_j$ .



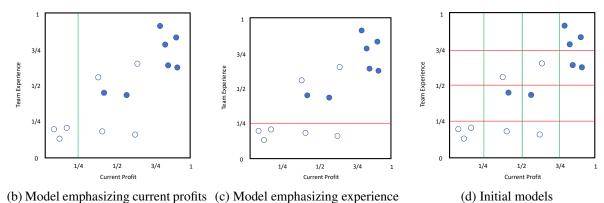


Figure A.1: Predicting the success of a startup

interpretations with others who have similar initial reactions to the data. Optimists who believe the data suggest that the average startup is likely to be successful talk to each other; pessimists who believe the data suggest that the average startup is likely to be *un*successful talk to each other; and moderates who believe that success of the average startup is 50-50 talk to each other. This community structure may emerge because people with different initial reactions have different objectives going forward. For instance, optimists think they are likely to invest and want to figure out the characteristics that matter most for success, while pessimists want to figure out the most compelling way to explain to their clients why they are not investing.

Social learning will lead beliefs to converge within each community to the model within that community that best fits the data. For instance, consider the optimists. Two models

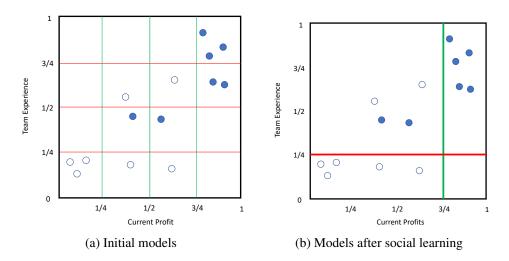


Figure A.2: Evolution of Beliefs Across Shared-Belief Networks Surrounding Startup Success

lead to optimistic interpretations of the data: one where the cutoff is at the 25th percentile of experience and one where the cutoff is at the 25th percentile of profits. The former fits the data almost ten times better than the latter. This can be seen in by comparing Figures A.1b and A.1c. The experience-based model in Figure A.1c more effectively separates successes from failures than does the profit-based model in Figure A.1b.<sup>5</sup> Thus, after social learning, all optimists adopt the experience-based model, depicted by thick-red horizontal line in Figure A.2b. Given the data and this adopted model, simple application of the standard beta-binomial updating formula tells us that members of the optimist community forecast average startup success to be  $3/4 \cdot ((7+1)/(9+2)) + 1/4 \cdot (1/(5+2)) \approx .58$ . Essentially, they believe the best way to explain the data is that failure is relatively rare—only the startups with the least experienced management teams fail.

Members of the pessimist community go through a similar evolution. There are two models that lead to pessimistic interpretations: one with a cutoff at the 75th percentile of experience and one with a cutoff at the 75th percentile of profits. In this case, the profit-based model fits approximately ten times better than the experienced-based model,

<sup>&</sup>lt;sup>5</sup>Formally, the likelihood of the data under the experience-based model is proportional to  $(\int_0^1 (1-\theta)^5 d\theta) \cdot (\int_0^1 \theta^7 (1-\theta)^2 d\theta) \approx .00046$ , while the likelihood of the data under the profit-based model is proportional to  $(\int_0^1 (1-\theta)^3 d\theta) \cdot (\int_0^1 \theta^7 (1-\theta)^4) \approx .000063$ .

so pessimists converge to the model depicted by the thick-green vertical line in Figure A.2b. Given the data, members in the pessimist community forecast average startup success to be  $3/4 \cdot ((2+1)/(9+2)) + 1/4 \cdot ((5+1)/(5+2)) \approx .42$ , disagreeing strongly with the members of the optimists community.

Finally, consider the neutral community. Prior to social learning, the two models in the neutral community are the default model (that the success probability is the same regardless of characteristics) and the model where the success or failure of each previous startup was inevitable given individuating characteristics. The latter model fits the data perfectly, so members of the neutral community converge to it, while continuing to forecast average startup success to be .5.

The example highlights how interpretations evolve differently across communities. Members of different communities end up not only with different final beliefs about startup success probabilities, but also disagreeing about the characteristics that matter for success. In the optimist community, some initially believe experience matters, while others initially believe profit matters. Yet all come to believe that startup success is predicted by experience and not profit. Members of the pessimist community similarly start out disagreeing, but instead come to believe that startup success is predicted by profits and not experience. In the neutral community, everyone comes to believe that success is unpredictable ex ante because individuating characteristics are all that matter.

In the example, sharing models in shared-belief communities does not result in muting optimists end up more optimistic after sharing models than they were on average before sharing models and similarly pessimists end up more pessimistic on average. Here we show using simulations that muting does appear to hold on average in the example, just not for the particular realization of the data we consider above. In each simulation, we first choose a value for the true success probability for the startup  $\theta$  from a set of 40 values evenly distributed on [0, 1]. We then randomly draw 5 startups with 3 characteristics: (i) success or failure with success having probability  $\theta$ , (ii) profit, which is uniformly distributed on [0, 1], and (iii) team experience, which is also uniformly distributed on [0, 1]. We consider models to explain success or failure that are cutoff rules in either profit or team experience. Five cutoff rules are considered, evenly spaced on each dimension. We compute the fit for all models, including the default model that the success probability is constant across characteristics. We then select the best-fitting model for optimists, i.e., the best-fitting model that implies an average posterior expected probability of success  $\hat{\theta}$  greater than 0.5, and the best-fitting model for pessimists, i.e., the best-fitting model that implies  $\hat{\theta}$  less than 0.5. For each value of the true success probability  $\theta$ , we average the optimists'  $\hat{\theta}$  and the pessimists'  $\hat{\theta}$  over 5000 simulations.

Figure A1 reports the results. We see that relative to the updating that would have taken place under the default model, there appears to be muting for both optimists and pessimists on average. In other words, for any value of  $\theta$ , the average optimists'  $\hat{\theta}$  and the average pessimists'  $\hat{\theta}$  is at least as close to the prior average of 0.5 as the average  $\hat{\theta}$  under the default model.

# **D** StockTwits Application Details

In this section, we provide regression evidence to supplement our analysis of StockTwits data in Section 6.2 of the main paper. We start with the universe of StockTwits messages studied by Divernois and Filipovic (2022), covering the period between January 2011 and July 2018. For each message about a particular stock, we code sentiment as 1 if the user labels the message as bullish and 0 if the user labels the message as bearish. We drop messages that users do not label. We restrict the sample to windows from 10 days before an earnings announcement to 10 days after for a given stock and restrict attention to users who have ever posted a message about that stock prior to 10 days before the earnings announcement. We code a user as a bull on the stock if the user labeled as bullish at least 50% of their messages about the stock prior to 10 days before the earnings announcement. We code the user as a bear if they labeled as bearish less than 50% of their messages about the stock. We then track how sentiment evolves in response to different earnings announcements over the surrounding windows. We code an announcement as positive news if the announcement day return is greater or equal to zero and as negative news if the announcement day return is negative.<sup>6</sup> The final sample consists of roughly 1.8 million messages across 40 thousand earnings announcements from 65 thousand unique users.

Table A1 presents regression evidence corresponding to Figure 4a in the main paper. Among the sample of users who are bullish on stock s for earnings announcement q, we

<sup>&</sup>lt;sup>6</sup>Announcement days are therefore defined as the first day that the stock can be traded following the announcement. For announcements that occur after the market close on a given day, the announcement day is then coded as the following day.

estimate the following regression:

$$1[Bullish]_{i,u,t,s,q} = \alpha + \sum_{l=-10}^{10} \beta_l 1[l=t] + \sum_{l=-10}^{10} \gamma_l 1[l=t] 1[NegativeSurprise_{s,q}] + \varepsilon_{i,u,t,s,q},$$
(A.1)

where

- $1[Bullish]_{i,u,t,s,q}$  is an indicator that tweet i by user u on event-day t is bullish and
- 1[NegativeSurprise<sub>s,q</sub>] is an indicator that the earnings announcement was a negative surprise.

Standard errors are reported in parentheses and clustered by year-month, stock, and user.

The first column replicates Figure 4a, weighting the data so that each earnings announcement is equally weighted. Note that to match the levels of Figure 4a, the constant in the regression must be added back in. The key coefficients are  $\gamma_{-1}$  and  $\gamma_0$ , which show that the sentiment of bullish investors declines substantially around negative earnings announcements, and  $\gamma_1$  to  $\gamma_{10}$ , which show that this decline is transient. The remaining columns show the robustness of the result. In the second column, we weight tweets equally rather than equal-weighting announcements. This has the effect of placing greater weight on announcements with more tweets. The remaining columns add fixed effects for the year-month of the announcement, the announcement itself, and the user interacted with the announcement. Across these variations, the basic pattern remains, though it weakens somewhat in the last column. The sentiment of bullish investors declines substantially around negative earnings announcements and then rebounds.

Table A2 presents regression evidence corresponding to Figure 4b in the main paper. Estimating Eq. (A.1) among the sample of users who are bearish on stock s for earnings announcement q, we find that bearish investors become less bearish around positive earnings announcements but then quickly revert.

### E How and When to Hold a Meeting

We consider a similar setting to Dessein and Santos (2006) and Bolton et al. (2013), closely following the latter paper's language and formulation. The environment is parameterized

by  $\omega \in [0, 1]$ , which is not known by the leader or a continuum of followers. Instead, they have a uniform prior over  $\omega$  and interpret data h in terms of what it implies about  $\omega$ .

The timing of the game is: (1) everyone observes h, (2) the leader announces the organization's strategy  $a_L \in [0, 1]$  and perhaps holds a meeting to discuss it in light of h, (3) each follower  $i \in [0, 1]$  chooses an action  $a_i \in [0, 1]$ , and (4) payoffs are realized. Each follower i has payoff:

$$-\alpha \cdot (a_i - [l_i \cdot a_L + (1 - l_i) \cdot \omega])^2 - \kappa \int_j (a_j - \bar{a})^2 dj,$$

where  $\alpha > 0$ ,  $\kappa > 0$ ,  $l_i \in [0, 1]$  and  $\bar{a} \equiv \int a_j dj$ . That is, each follower values (i) taking an action that is aligned with a weighted average of the organization's strategy  $a_L$  and the environment  $\omega$  and (ii) coordinating with others. To limit the number of cases, assume that  $l_i = 0$  for almost all followers and  $l_i = 1$  for positive fraction  $\varepsilon \to 0$  of followers.<sup>7</sup> That is, almost all followers care about taking an action that is well-adapted to the environment, rather than than taking an action that is aligned with the organization's strategy, and the rest of the followers mechanically follow the organization's strategy. Since it focuses on the case where  $l_i = 0$  for fraction  $(1 - \varepsilon) \approx 1$  of followers, the analysis better applies to situations where workers care more about getting things right than about following the leader. The leader's payoff simply aggregates the followers' payoffs:<sup>8</sup>

$$-\alpha \int_{i} (a_i - [l_i \cdot a_L + (1 - l_i) \cdot \omega])^2 di - \kappa \int_{j} (a_j - \bar{a})^2 dj.$$

The leader and followers share the same default model. While the leader is dogmatic the default is correct, followers may move away from it by sensemaking with fellow followers. Because  $\Omega$  in this example is the full unit interval, we for simplicity limit the set of

<sup>&</sup>lt;sup>7</sup>Having some followers mechanically follow the organization's strategy induces a cost to the leader of announcing a different strategy from what she thinks is subjectively optimal. There are other ways to generate such a cost, e.g., by assuming that followers and leaders value an organization that is well-adapted to its environment as Bolton et al. (2013) do. Our approach is analytically simple, but our qualitative results do not hinge on our precise formulation.

<sup>&</sup>lt;sup>8</sup>For simplicity, we assume the leader evaluates her expected payoff according to her own expectation and not followers' subjective expectations. The leader has an incentive for followers' actions to be well-adapted to the leader's view of the environment, but does not directly care whether the followers believe their actions are well-adapted. Introducing the latter force could provide another reason to hold meetings in our framework: to get followers on board with the direction of the organization, even when getting followers on board does not influence their actions.

models M followers could consider to be finite. We assume M always includes (i) the default model d, (ii) the best-fitting model  $m^{bf}$  that induces the same beliefs as d (i.e.,  $\mu(h, m^{bf}) = \mu(h, d)$ ), (iii) a model that says the history is inevitable in hindsight (i.e., a model m such that  $\Pr(h|m, \mu_0) = 1$ ), and (iv) at least one model m with a fit between the default's and the best-fitting model's:  $\Pr(h|m, \mu_0) \in (\Pr(h|d, \mu_0), \Pr(h|m^{bf}, \mu_0))$  and  $\mu(h, m) \neq \mu(h, d)$ . For simplicity, we also assume that  $m^{bf}$  fits better than all models in M except for the model that says the history is inevitable in hindsight.

If the leader does not hold a meeting, then workers make sense of h in their own communities. Holding a meeting costs the leader a positive amount c that is vanishingly small. By holding a meeting, the leader is able to perfectly control the set of models each worker is exposed to,  $M_i$ , by influencing the flow of communication between followers.

#### **Proposition A.4.** In the leader-follower example:

- If information h is closed to interpretation or followers always stick with their default interpretation of the information absent persuasion (δ = 1), the leader never holds a meeting. In this case, a<sub>L</sub> = E<sub>μ(h,d)</sub>[ω] for all h, and a<sub>i</sub> = a<sub>L</sub> for all i.
- 2. Otherwise, the leader may hold a meeting.
  - (a) If the weight placed on coordination ( $\kappa$ ) is sufficiently large or if h is uninformative under the default model in the sense that  $\mathbb{E}_{\mu(h,d)}[\omega] = \mathbb{E}_{\mu_0}[\omega] \equiv \omega_0$ , then the leader calls a meeting whenever some followers take an action other than  $\omega_0$  absent a meeting. In this case (i) an optimal meeting features open communication ( $M_i = M$  for all i), (ii)  $a_L = \omega_0$ , and (iii)  $a_i = \omega_0$  for all i.
  - (b) If the weight placed on adaptation ( $\alpha$ ) is sufficiently large and followers should react to the information under the default model in the sense that  $\mathbb{E}_{\mu(h,d)}[\omega] \neq \mathbb{E}_{\mu_0}[\omega]$ , then the leader calls a meeting whenever too many followers take an action other than  $\mathbb{E}_{\mu(h,d)}[\omega]$  absent a meeting. In this case (i) an optimal meeting features directed communication with  $M_i \neq M$ , (ii)  $a_L \neq \omega_0$ , and (iii) not all followers take the same action.

*Proof of Proposition A.4.* For the first case, it's obvious that the leader never holds a meeting because holding a meeting costs c > 0 and does not influence beliefs and decisions

when information is closed to interpretation or when followers always stick with their default interpretation of the information absent persuasion. Since  $a_L = \mathbb{E}_{\mu(h,d)}[\omega]$  implies  $a_i = a_L$  for all *i* (this is obvious for followers who blindly follow  $a_L$  and other followers set  $a_i = l \cdot a_L + (1-l) \cdot \mathbb{E}_{\mu(h,d)}[\omega] = a_L$ ), it remains to show in this case that  $a_L = \mathbb{E}_{\mu(h,d)}[\omega]$ . Setting  $a_L = \mathbb{E}_{\mu(h,d)}[\omega]$  uniquely maximizes the coordination term,  $-\int_j (a_j - \bar{a})dj$ , of the leader's payoff since everyone coordinates on  $a_L$ . Since simple algebra shows that  $a_L$ doesn't influence the adaptation term,  $\int_i -(a_i - [l_i \cdot a_L + (1 - l_i) \cdot \omega])^2 di$ , it is optimal for the leader to set  $a_L = \mathbb{E}_{\mu(h,d)}[\omega]$ .

For the first part of the second case, optimizing the leader's payoff becomes equivalent to maximizing the coordination term,  $\int_j (a_j - \bar{a})^2 dj$ , when the weight placed on coordination  $\kappa$  is sufficiently large. Given that a positive fraction of followers initially adopt the perfectly-fitting neutralizing model, the only way for all followers to perfectly coordinate their actions is for them all to take  $a_i = \omega_0$ . This is implemented by followers being exposed to all models, either with open communication absent a meeting or with open communication in a meeting. This is also optimal from the point of view of the leader when his uninformative under the default model in the sense that  $\mathbb{E}_{\mu(h,d)}[\omega] = \omega_0$ . The leader does better by holding a meeting than not whenever some followers would adopt a model that implies a belief other than  $\mu_0$  absent a meeting.

For the last part, if followers are exposed to all models ( $M_i = M$  for all *i*), then they perfectly coordinate their actions and the leader's payoff approximately equals

$$-\alpha \mathbb{E}_{\mu(h,d)} \int_{i} (a_{i} - \omega)^{2} di = -\alpha \mathbb{E}_{\mu(h,d)} \int_{i} (\omega_{0} - \omega)^{2} di,$$
(A.2)

since  $l_i = 0$  for almost all followers. If followers are instead all exposed to only models supporting  $a_i = \mathbb{E}_{\mu(h,d)}[\omega]$  (i.e.,  $M_i = \{d, m^{bf}\}$  for all *i*), then the leader's payoff approximately equals

$$-\alpha \left[ \mathbb{E}_{\mu(h,d)}\rho \int_{i} (\mathbb{E}_{\mu(h,d)}[\omega] - \omega)^{2} di + (1-\rho) \int_{i} (\omega_{0} - \omega)^{2} di \right] -\kappa \int_{j} (a_{j} - \rho \mathbb{E}_{\mu(h,d)}[\omega] - (1-\rho)\omega_{0})^{2} dj,$$
(A.3)

where  $\rho$  equals the fraction of followers who are persuadable by  $m^{bf}$  (i.e., fraction  $1 - \rho$  are the fraction with the initial reaction to adopt the perfectly-fitting neutralizing model). Since the first term of (A.3) is larger than (A.2) when  $\mathbb{E}_{\mu(h,d)}[\omega] \neq \omega_0$ , in this case the leader holds a meeting that features directed communication whenever  $\alpha$  is sufficiently large. Such a meeting will clearly be better than not holding a meeting whenever followers whose initial reaction to the data differs from  $\mu(h, d)$  are not exposed to  $m^{bf}$  absent a meeting or are exposed to the model that says the history is inevitable in hindsight.<sup>9</sup>

The first part of Proposition A.4 says that, when data is closed to interpretation or followers do not try to make sense of the data on their own, then there is no need for the leader to call a meeting to discuss the organization's strategic response to publicly available data. The leader just announces her strategic response, which varies one-for-one with the leader's reaction to the data.

The second part of the proposition shows that the leader's reaction is very different when data is open to interpretation and followers try to make sense of it on their own. Meetings then allow leaders to better control interpretations followers share with each other. If the leader thinks followers are reacting to data when they should not be, or if the leader highly values coordination, then she calls a meeting which features open communication: everyone shares their view of what the event means for the organization. While opinions will be voiced that the leader does not agree with, at the end of the day everyone will share a view that the event teaches them little that they did not already know. Thus, the status quo will prevail. In this case, the leader's strategic response to publicly available data may be different than her private response: if she believes that she cannot persuade enough followers of her desired course of action, her best alternative is to ensure coordination by structuring the meeting to neutralize the data. This may be one reason why informal (e.g., relational) contracts are "hard to build *and change*" (emphasis added, Gibbons and Henderson (2012)).

On the other hand, if too many followers are underreacting to the data or the leader strongly values adaptation, then the leader calls a meeting featuring a *persuasive campaign*.

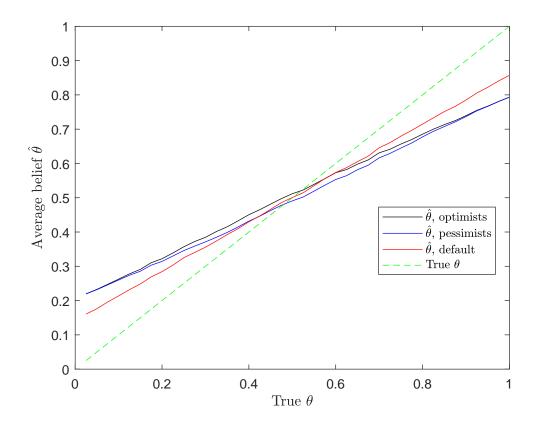
$$-\alpha\rho\mathbb{E}_{\mu(h,d)}\left[(\mathbb{E}_{\mu(h,d)}[\omega]-\omega)^2-(\omega_0-\omega)^2\right]-\kappa\left[\int_j(a_j-\rho\mathbb{E}_{\mu(h,d)}[\omega]-(1-\rho)\omega_0)^2dj\right]$$

<sup>&</sup>lt;sup>9</sup>To see when else the leader wants to hold such a meeting, (A.3) minus (A.2) equals:

which, after some algebra, equals  $\alpha \rho(\mathbb{E}_{\mu(h,d)}[\omega] - \omega_0)^2 - \kappa \rho(1-\rho)(\mathbb{E}_{\mu(h,d)}[\omega] - \omega_0)^2$ . So a meeting featuring directed communication is optimal whenever  $\alpha > \kappa(1-\rho)$ . This reveals that a leader is more likely to call a meeting to encourage followers to take an action different from  $\omega_0$  the greater the fraction of followers who are persuadable to take such an action—that is, the smaller the fraction of followers who, prior to the meeting, are hardened in their views that the data tells them little they didn't already know.

The leader ensures that the loudest voices are those with interpretations consistent with her view of the optimal action  $\mathbb{E}_{\mu(h,d)}[\omega]$ . While not everyone ends up on board with the shift in strategy from the status quo  $\omega_0$ , as many as possible will be on board. Per Proposition 4 there is also a motive to hold the meeting as soon as possible, before workers can share interpretations with each other on their own.

#### Figure A1: Muting in the VC Example



*Notes*: This figure suggests that muting obtains on average in the VC example. For each of 40 different values of the true probability of success,  $\theta$ , we simulate data on a history of 5 startups, each of which varies in their profit and team experience. VCs entertain models that are cutoff rules on each dimension. The figure plots the average posterior expectation of the success probability,  $\hat{\theta}$ , of VCs under three models against the true success probability: the default model (red line), the model adopted after optimists share interpretations, and the model adopted after pessimists share. interpretations. The figure averages over 5000 simulations for each value of  $\theta$ .

	(1)	(2)	(3)	(4)	(5)
t=-9	0.01	-0.01	0.01	0.00	0.00
	(1.13)	(-0.96)	(1.19)	(0.97)	(1.44)
t=-8	0.00	-0.00	0.00	0.00	0.00
	(0.04)	(-0.62)	(0.16)	(0.27)	(1.15)
t=-7	0.01	-0.00	0.01	0.01*	0.01
	(1.16)	(-0.94)	(1.39)	(1.76)	(1.40)
t=-6	0.01*	0.00	0.01**	0.01**	0.00
	(1.72)	(0.28)	(2.00)	(2.13)	(1.15)
t=-5	0.01**	0.00	0.01**	0.01**	0.01**
	(2.13)	(0.06)	(2.43)	(2.51)	(2.56)
t=-4	0.01	-0.01*	0.01	0.01	0.01*
	(1.20)	(-1.80)	(1.59)	(1.39)	(1.70)
t=-3	0.01	-0.00	0.01**	0.01*	0.01*
	(1.66)	(-0.67)	(2.13)	(1.72)	(1.96)
t=-2	0.01	-0.00	0.01	0.00	0.01**
	(0.96)	(-0.70)	(1.53)	(1.00)	(2.58)
t=-1	0.00	-0.01	0.01	0.01	0.01**
	(0.36)	(-1.46)	(0.95)	(1.42)	(3.27)
t=0	0.01	-0.01**	0.01	0.01*	0.01**
	(0.80)	(-2.02)	(1.58)	(1.91)	(3.39)
t=1	-0.01*	-0.02**	-0.01	-0.01	0.01**
	(-1.87)	(-4.75)	(-1.18)	(-1.24)	(2.33)
t=2	-0.01	-0.01**	-0.00	-0.00	0.01*
	(-1.32)	(-2.10)	(-0.58)	(-0.32)	(1.75)
t=3	-0.01	-0.02**	0.00	-0.00	0.01**
	(-0.74)	(-2.38)	(0.04)	(-0.24)	(2.38)
t=4	-0.00	-0.01*	0.00	0.00	0.01*
	(-0.29)	(-1.68)	(0.60)	(0.42)	(1.72)
t=5	-0.00	-0.01**	0.01	0.00	0.01**
1-5	(-0.05)	(-2.09)	(0.73)	(0.51)	(2.07)
t=6	-0.01	-0.02**	-0.00	-0.00	0.01**
1=0	(-1.58)	(-3.07)	(-0.57)	(-0.85)	(2.20)
t=7	-0.02*	-0.01**	-0.01	-0.00	0.01**
(_/	(-1.97)	(-2.16)	(-1.02)	(-0.59)	(2.54)
t=8	-0.01*	-0.01**	-0.00	-0.00	(2.34)
1-0				(-0.40)	
t-0	(-1.79)	(-2.45) -0.02**	(-0.57) 0.00	0.01	(2.62) 0.02**
t=9	-0.00				
t_10	(-0.58)	(-2.52)	(0.66)	(1.34)	(2.97) 0.02**
t=10	0.00	-0.00	0.01*	0.01*	
4 10 · · •	(0.46)	(-0.23)	(1.81)	(1.87)	(4.12)
$t=-10 \times \text{Neg}$	-0.02**	-0.02**	-0.02**	-0.03**	-0.02**
	(-2.75)	(-2.25)	(-3.03)	(-4.93)	(-4.51)
$t=-9 \times \text{Neg}$	-0.03**	-0.02**	-0.03**	-0.04**	-0.03**
	(-3.77)	(-3.22)	(-3.92)	(-6.60)	(-6.83)
$t=-8 \times Neg$	-0.03**	-0.01**	-0.03**	-0.03**	-0.03**

Table A1: Bulls' Beliefs around Earnings Announcements

	(-2.86)	(-2.68)	(-2.93)	(-5.56)	(-6.26)
$t=-7 \times Neg$	-0.04**	-0.02**	-0.04**	-0.04**	-0.03**
	(-4.73)	(-4.00)	(-4.62)	(-6.82)	(-5.83)
$t=-6 \times Neg$	-0.04**	-0.03**	-0.04**	-0.04**	-0.03**
	(-5.83)	(-5.55)	(-5.44)	(-7.65)	(-5.69)
$t=-5 \times Neg$	-0.04**	-0.04**	-0.04**	-0.04**	-0.03**
	(-5.71)	(-5.80)	(-5.21)	(-5.78)	(-4.99)
$t=-4 \times Neg$	-0.05**	-0.04**	-0.05**	-0.05**	-0.03**
	(-6.87)	(-5.94)	(-6.26)	(-8.16)	(-6.85)
$t=-3 \times Neg$	-0.05**	-0.04**	-0.05**	-0.05**	-0.03**
	(-5.17)	(-4.93)	(-4.85)	(-6.28)	(-6.44)
$t=-2 \times Neg$	-0.06**	-0.04**	-0.05**	-0.06**	-0.03**
	(-5.80)	(-5.42)	(-5.50)	(-8.39)	(-6.44)
$t=-1 \times Neg$	-0.09**	-0.06**	-0.09**	-0.08**	-0.04**
	(-5.63)	(-7.10)	(-5.55)	(-8.34)	(-8.40)
$t=0 \times Neg$	-0.10**	-0.06**	-0.10**	-0.08**	-0.03**
	(-7.60)	(-8.96)	(-7.25)	(-9.72)	(-7.43)
$t=1 \times Neg$	-0.03**	-0.04**	-0.03**	-0.03**	-0.01**
	(-4.34)	(-5.53)	(-3.63)	(-5.56)	(-3.07)
$t=2 \times Neg$	-0.00	-0.00	0.00	-0.01	-0.01
	(-0.60)	(-0.63)	(0.12)	(-1.32)	(-1.21)
$t=3 \times Neg$	-0.00	0.00	0.00	-0.01	-0.01
	(-0.26)	(0.32)	(0.48)	(-1.53)	(-1.63)
$t=4 \times Neg$	-0.00	0.00	0.00	-0.01	-0.01
	(-0.08)	(0.17)	(0.44)	(-1.29)	(-1.58)
$t=5 \times Neg$	0.00	0.00	0.01	-0.00	-0.01**
	(0.62)	(1.08)	(1.13)	(-0.90)	(-2.05)
$t=6 \times Neg$	0.00	-0.00	0.01	-0.00	-0.00
	(0.41)	(-0.41)	(1.18)	(-0.28)	(-0.51)
$t=7 \times Neg$	0.00	-0.00	0.01	-0.00	-0.00
	(0.39)	(-0.62)	(1.26)	(-0.16)	(-0.91)
$t=8 \times Neg$	-0.00	-0.01*	0.00	-0.00	-0.00
	(-0.40)	(-1.72)	(0.64)	(-0.68)	(-0.83)
$t=9 \times Neg$	-0.00	-0.01	0.00	0.00	-0.00
	(-0.37)	(-1.08)	(0.56)	(0.17)	(-0.95)
$t=10 \times Neg$	-0.00	-0.01	0.00	0.00	0.00
	(-0.57)	(-0.78)	(0.60)	(.)	(.)
Constant	0.94**	0.96**	0.93**	0.94**	0.94**
	(124.89)	(262.61)	(127.29)	(291.92)	(428.90)
Weighting	Event	Tweet	Event	Event	Event
Fixed Effects			YM	Event	User x Event
	010	0076	010	.27	.77
$R^2$	.013	.0076	.019	.27	.//

*Notes*: This table presents the evolution of bulls' beliefs around positive and negative earnings announcements. The sample is all tweets within 10 days of an earnings announcement by users who have tweeted at

least once about the stock before the  $\pm 10$ -day window, with more than 50% of these prior tweets self-labeled as bullish. Let *s* denote the stock, *q* denote the announcement event (quarter), *t* denote the day relative to the event (ranging from -10 to 10 with t = 0 corresponding to the event date). The dependent variable is an indicator that a tweet on event-day *t* for stock *f* and event *q* is self-labeled as bullish. The independent variables are dummies for *t*, interacted with dummies indicating that the earnings announcement was negative, measured by negative announcement day returns. The event date (t = 0) is defined as the first day the news is tradeable. The Weighting row indicates whether the regression is weighted to equal-weight each event or unweighted (i.e., each tweet is weighted equally). Standard errors are reported in parentheses and clustered by year-month, stock, and user.

	(1)	(2)	(3)	(4)	(5)
t=-9	0.01	-0.00	0.01	0.00	-0.03
	(0.30)	(-0.06)	(0.34)	(0.11)	(-1.48)
t=-8	-0.02	-0.01	-0.02	-0.01	-0.01
	(-0.78)	(-0.14)	(-0.79)	(-0.51)	(-1.09)
t=-7	0.04	0.01	0.04*	0.03	-0.01
	(1.61)	(0.23)	(1.67)	(1.36)	(-1.10)
t=-6	0.03	0.01	0.03	0.00	0.00
	(1.45)	(0.28)	(1.27)	(0.18)	(0.04)
t=-5	0.06**	0.03	0.05**	0.02	-0.01
	(2.28)	(1.06)	(2.10)	(0.78)	(-0.36)
t=-4	0.07**	0.00	0.06**	0.01	-0.02
	(2.54)	(0.02)	(2.26)	(0.36)	(-0.96)
t=-3	0.06**	0.03	0.05*	0.02	-0.00
	(2.16)	(0.82)	(1.79)	(0.59)	(-0.13)
t=-2	0.08**	0.05	0.07**	0.03	0.00
	(3.08)	(1.13)	(2.71)	(1.53)	(0.36)
t=-1	0.10**	0.04	0.09**	0.02	-0.01
	(3.28)	(1.17)	(2.96)	(0.82)	(-1.17)
t=0	0.11**	0.05	0.09**	0.01	-0.02*
	(3.14)	(1.34)	(2.84)	(0.56)	(-1.92)
t=1	-0.01	-0.02	-0.02	-0.06**	-0.05**
	(-0.34)	(-0.70)	(-0.82)	(-2.66)	(-3.43)
t=2	-0.04	-0.05	-0.05*	-0.07**	-0.05**
	(-1.34)	(-1.61)	(-1.80)	(-2.95)	(-3.51)
t=3	-0.02	-0.05	-0.03	-0.06**	-0.05**
	(-0.78)	(-1.63)	(-1.26)	(-2.52)	(-2.78)
t=4	-0.05*	-0.06	-0.07**	-0.08**	-0.06**
	(-1.88)	(-1.66)	(-2.50)	(-3.25)	(-3.23)
t=5	-0.04	-0.05*	-0.05**	-0.07**	-0.05**
	(-1.65)	(-1.68)	(-2.33)	(-3.47)	(-2.80)
t=6	-0.05*	-0.09**	-0.06**	-0.09**	-0.05**
	(-1.94)	(-2.67)	(-2.66)	(-3.60)	(-2.87)
t=7	-0.08**	-0.11**	-0.10**	-0.10**	-0.07**
. ,	(-2.86)	(-3.13)	(-3.71)	(-3.87)	(-3.80)
t=8	-0.09**	-0.12**	-0.11**	-0.12**	-0.08**
1-0	(-3.27)	(-3.18)	(-4.17)	(-5.07)	(-4.01)
t=9	-0.08**	-0.11**	-0.10**	-0.12**	-0.08**
(=)	(-2.49)	(-3.32)	(-3.34)	(-4.30)	(-3.71)
t=10	-0.10**	-0.12**	-0.12**	-0.14**	-0.09**
-10	(-3.23)	(-3.28)	-0.12 (-4.31)	(-5.62)	-0.09
t=-10 $\times$ Neg	(-3.23) -0.06**	-0.08**	(-4.31) -0.06**	(-3.62)	0.00
$1 - 10 \times 10$	(-2.36)		(-2.05)		(0.24)
t=-9 $\times$ Neg	(-2.30) -0.09**	(-2.43) -0.05	-0.08**	(2.00) 0.01	
$i = -9 \times \text{Ineg}$					-0.00
+_ 0 \/ NT	(-3.36)	(-1.60)	(-2.96)	(0.56)	(-0.17)
$t=-8 \times Neg$	-0.07**	-0.06	-0.07**	0.02	-0.01

Table A2: Bears' Beliefs around Earnings Announcements

	(-2.85)	(-1.42)	(-2.47)	(1.10)	(-0.32)
$t=-7 \times Neg$	-0.08**	-0.08**	-0.08**	0.03	0.01
	(-3.29)	(-2.19)	(-3.06)	(1.28)	(0.61)
$t=-6 \times \text{Neg}$	-0.07**	-0.07*	-0.07**	0.03	0.01
	(-2.82)	(-1.87)	(-2.75)	(1.45)	(0.77)
$t=-5 \times Neg$	-0.09**	-0.08**	-0.09**	0.01	-0.01
	(-3.52)	(-2.03)	(-3.58)	(0.60)	(-0.40)
$t=-4 \times Neg$	-0.10**	-0.10**	-0.10**	-0.00	-0.01
	(-3.50)	(-2.80)	(-3.59)	(-0.10)	(-0.54)
$t=-3 \times Neg$	-0.08**	-0.10**	-0.08**	0.02	-0.00
	(-3.09)	(-2.58)	(-3.13)	(0.91)	(-0.14)
$t=-2 \times Neg$	-0.09**	-0.10**	-0.10**	-0.00	-0.02
	(-3.65)	(-2.74)	(-3.60)	(-0.15)	(-0.96)
$t=-1 \times Neg$	-0.11**	-0.11**	-0.12**	-0.03	-0.03
	(-4.43)	(-3.06)	(-4.76)	(-1.53)	(-1.64)
$t=0 \times Neg$	-0.13**	-0.14**	-0.14**	-0.05**	-0.02
	(-5.32)	(-3.88)	(-5.56)	(-2.87)	(-1.63)
$t=1 \times Neg$	-0.06**	-0.10**	-0.07**	0.01	-0.01
	(-2.13)	(-2.60)	(-2.57)	(0.49)	(-0.29)
$t=2 \times Neg$	-0.01	-0.07*	-0.02	0.07**	0.01
	(-0.45)	(-1.79)	(-0.93)	(3.67)	(0.70)
$t=3 \times Neg$	-0.01	-0.05	-0.02	0.07**	0.02
	(-0.40)	(-1.26)	(-0.78)	(3.97)	(0.94)
$t=4 \times Neg$	-0.02	0.01	-0.02	0.06**	0.00
	(-0.67)	(0.13)	(-0.82)	(2.83)	(0.12)
$t=5 \times Neg$	-0.02	-0.04	-0.03	0.06**	0.01
	(-0.57)	(-1.05)	(-0.98)	(2.42)	(0.47)
$t=6 \times Neg$	-0.04*	-0.08**	-0.06**	0.04**	0.01
	(-1.95)	(-2.22)	(-2.36)	(2.10)	(0.56)
$t=7 \times Neg$	-0.05*	-0.07**	-0.06**	0.03	-0.00
	(-1.86)	(-2.00)	(-2.51)	(1.57)	(-0.08)
$t=8 \times Neg$	-0.05**	-0.09**	-0.07**	0.02	-0.01
	(-2.02)	(-2.63)	(-2.67)	(0.85)	(-0.61)
$t=9 \times Neg$	-0.10**	-0.12**	-0.12**	-0.02	-0.02
	(-3.15)	(-3.35)	(-4.06)	(-0.92)	(-1.42)
$t=10 \times Neg$	-0.08**	-0.16**	-0.11**	0.00	0.00
	(-2.91)	(-4.61)	(-3.65)	(.)	(.)
Constant	0.37**	0.34**	0.38**	0.33**	0.32**
	(14.59)	(10.20)	(16.32)	(27.12)	(33.77)
$R^2$	0.02	0.02	0.04	0.43	0.81
N	220,280	220,280	220,280	213,854	187,869
Weighting	Event	Tweet	Event	Event	Event
Fixed Effects	2.011	1	YM	Event	User x Event
. Inca Eliceto			1 1/1	Lient	Ster A Event

*Notes*: This table presents the evolution of bears' beliefs around positive and negative earnings announcements. The sample is all tweets within 10 days of an earnings announcement by users who have tweeted at

least once about the firm before the  $\pm 10$ -day window, with more than 50% of these prior tweets self-labeled as bearish. Let f denote the firm, q denote the announcement event (quarter), t denote the day relative to the event (ranging from -10 to 10 with t = 0 corresponding to the event date). The dependent variable is an indicator that a tweet on event-day t for firm f and event q is self-labeled as bullish. The independent variables are dummies for t, interacted with dummies indicating that the earnings announcement was negative, measured by negative announcement day returns. The event date (t = 0) is defined as the first day the news is tradeable. The Weighting row indicates whether the regression is weighted to equal-weight each event or unweighted (i.e., each tweet is weighted equally). Standard errors are reported in parentheses and clustered by year-month, firm, and user.

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